

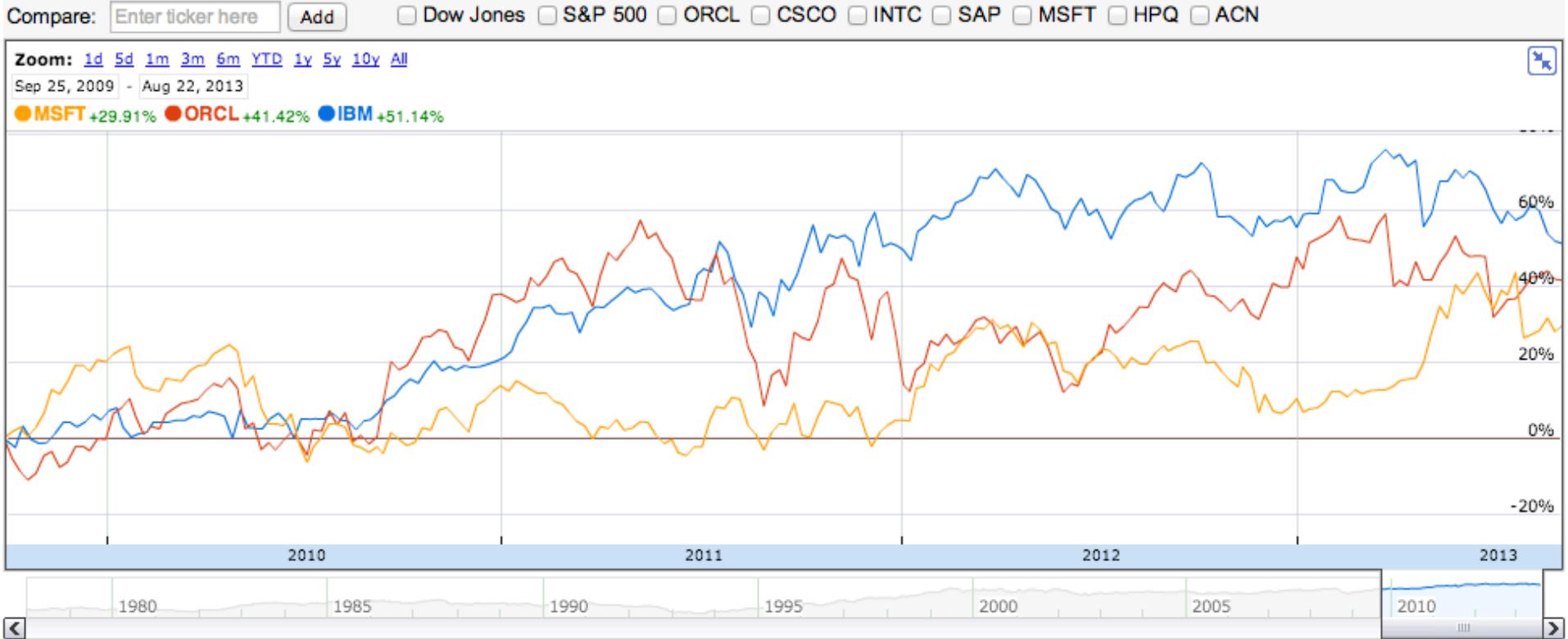
Scorpion

Explaining Away Outliers in Aggregate Queries

eugene wu and sam madden

MIT





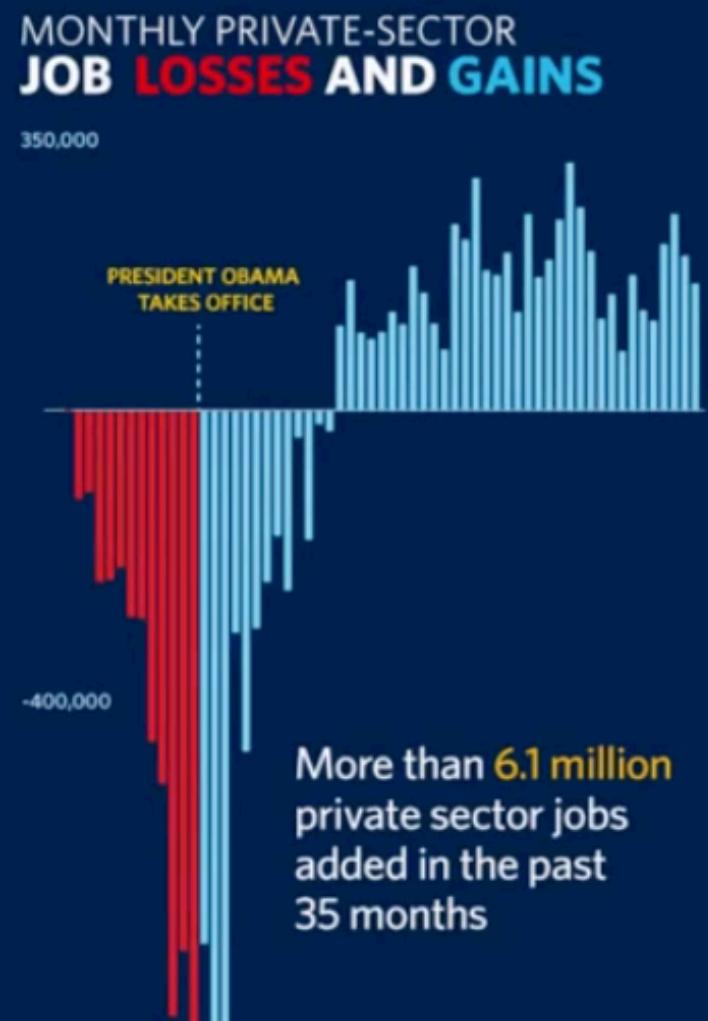


MONTHLY PRIVATE-SECTOR JOB LOSSES AND GAINS

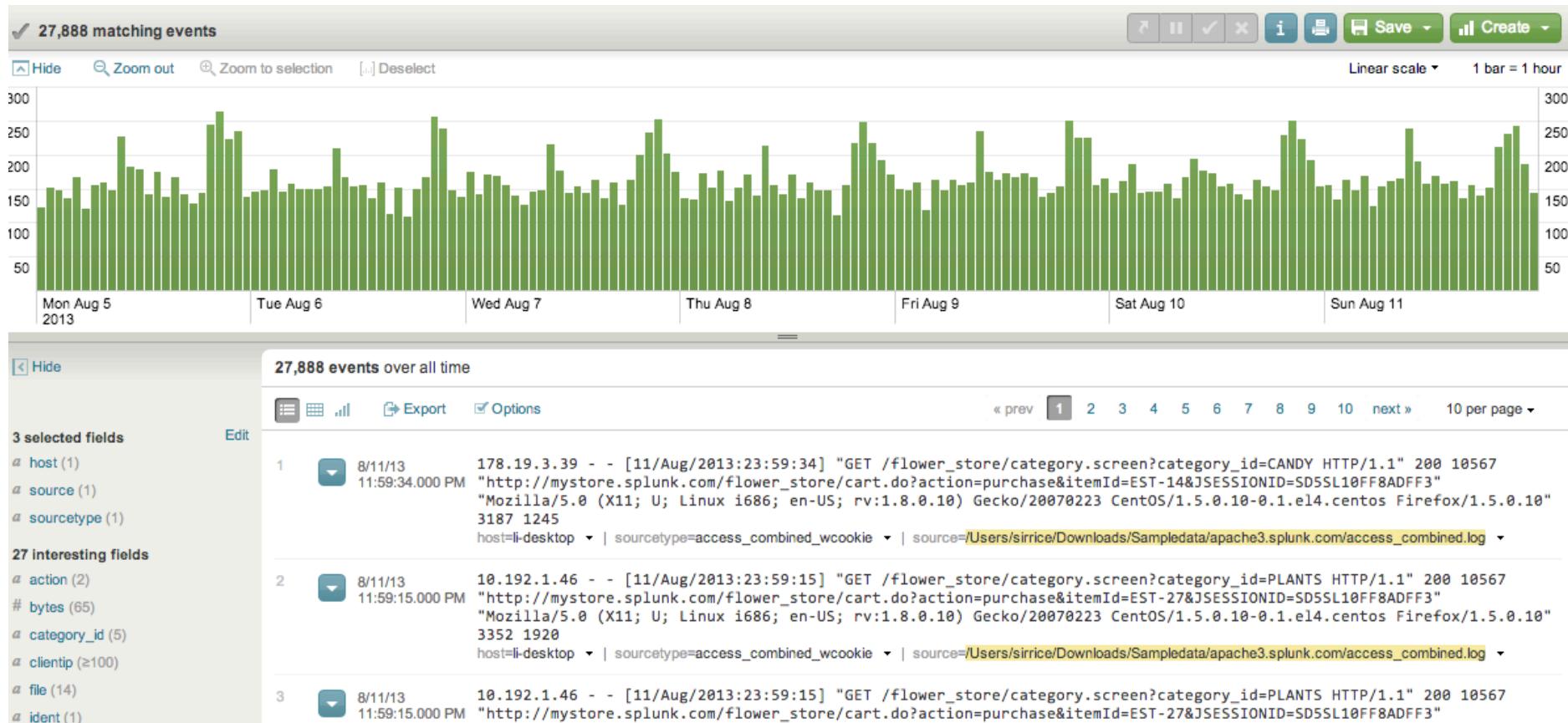
350,000

PRESIDENT OBAMA
TAKES OFFICE

-400,000



More than 6.1 million
private sector jobs
added in the past
35 months

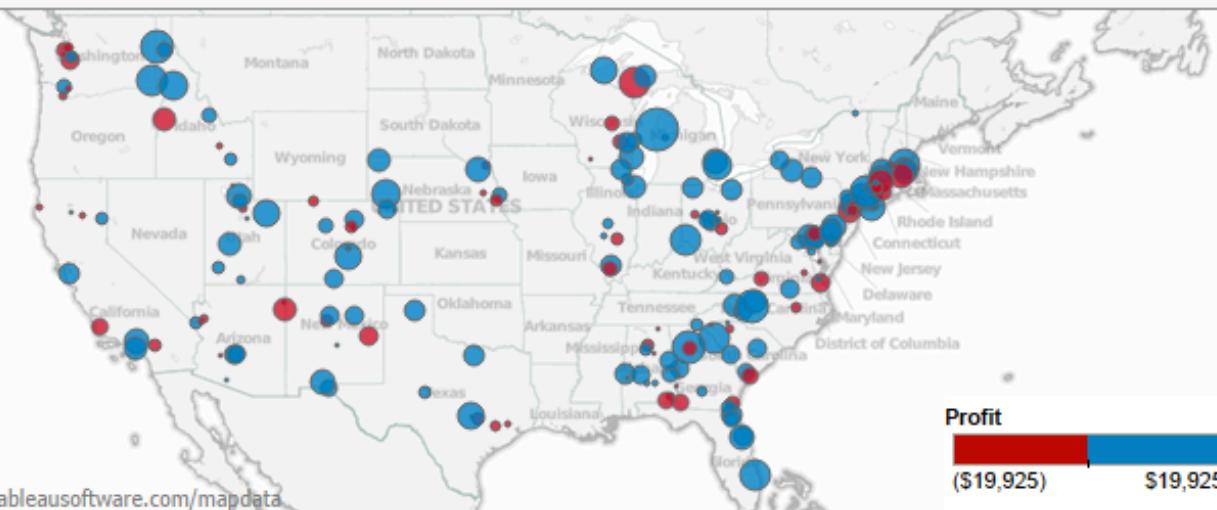


Executive Dashboard

Sales by Customer Location


Sales

- \$12
- \$20,000
- \$40,000
- \$60,000
- \$80,000
- \$103,506

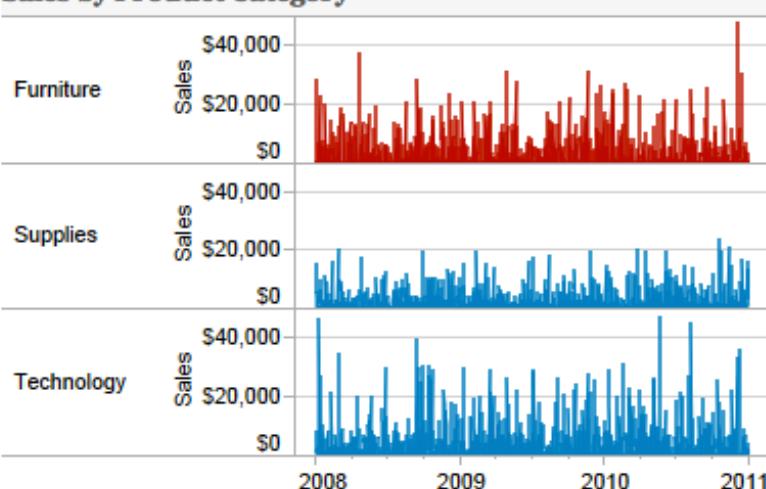

Select Year:

Customer Region:

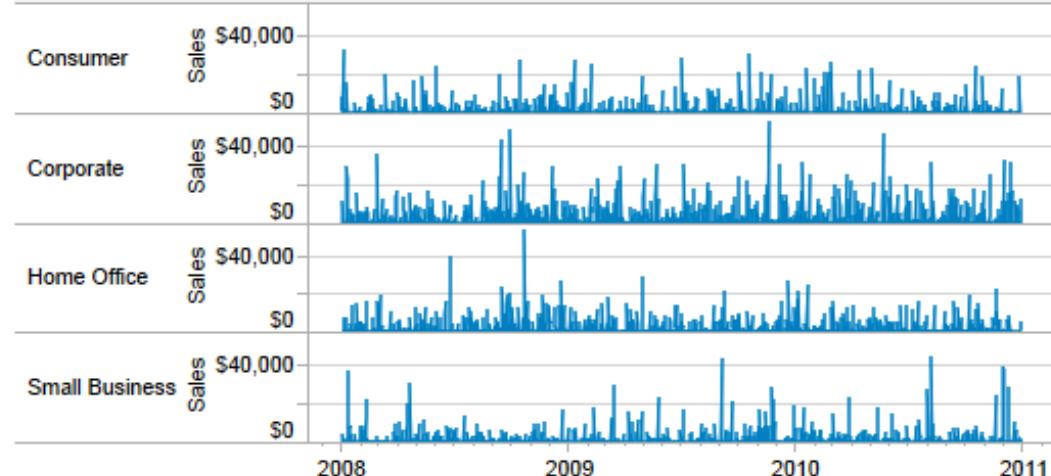
Product Category:

Customer Segment:

Sales by Product Category



Sales by Customer Segment



Find reports & more

MY STUFF

Dashboards

Shortcuts

Intelligence Events

STANDARD REPORTS

Real-Time

Audience

Overview

► Demographics

► Behavior

► Technology

► Mobile

► Custom

Visitors Flow

Traffic Sources

Content

Conversions

Audience Overview

Jul 17, 2013 - Aug 16, 2013 ▾

Advanced Segments

Email

Export ▾

Add to Dashboard

Shortcut

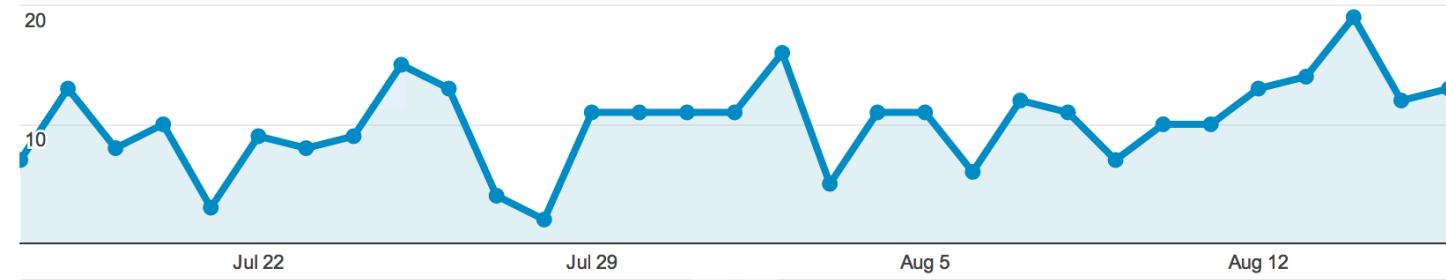
% of visits: 100.00%

Overview

Visits ▾ vs. Select a metric

Hourly Day Week Month

Visits



237 people visited this site

New Visitor Returning Visitor

Visits

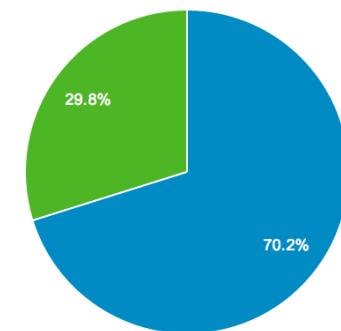
315

Unique Visitors

237

Pageviews

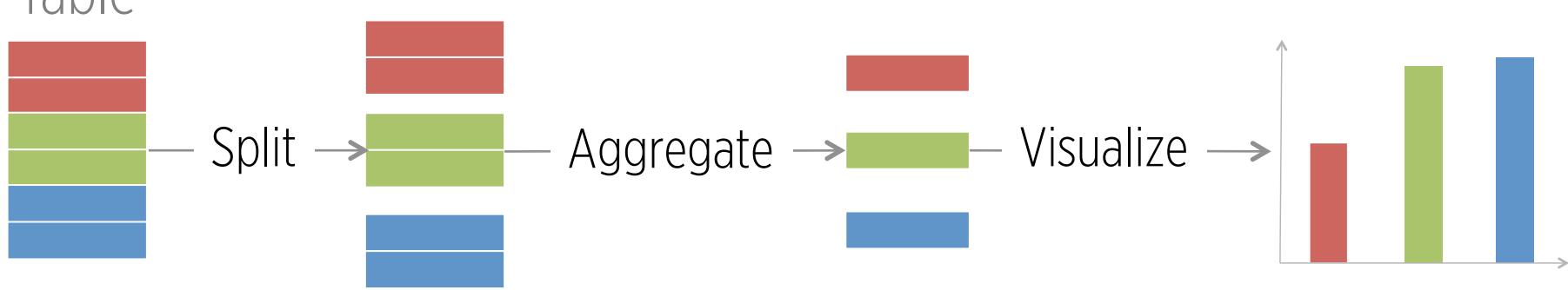
482

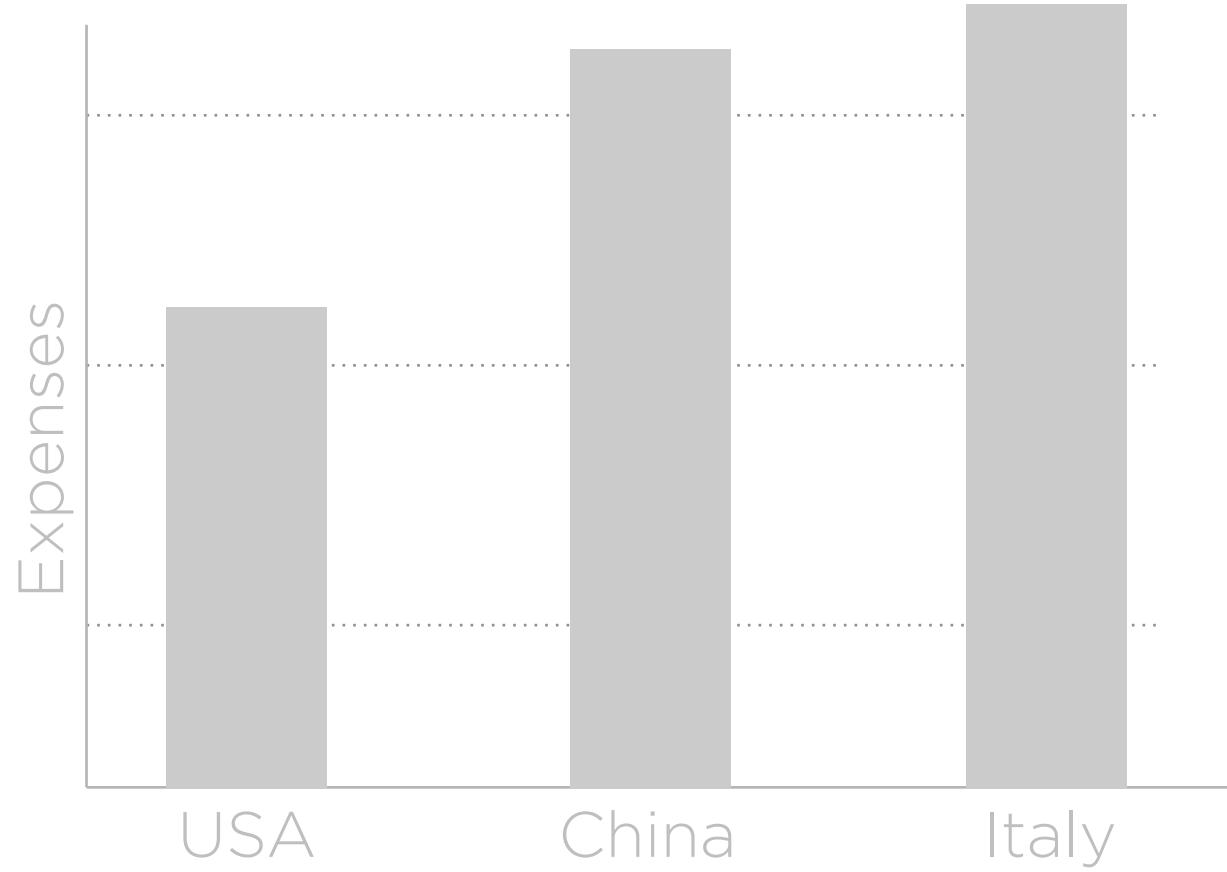




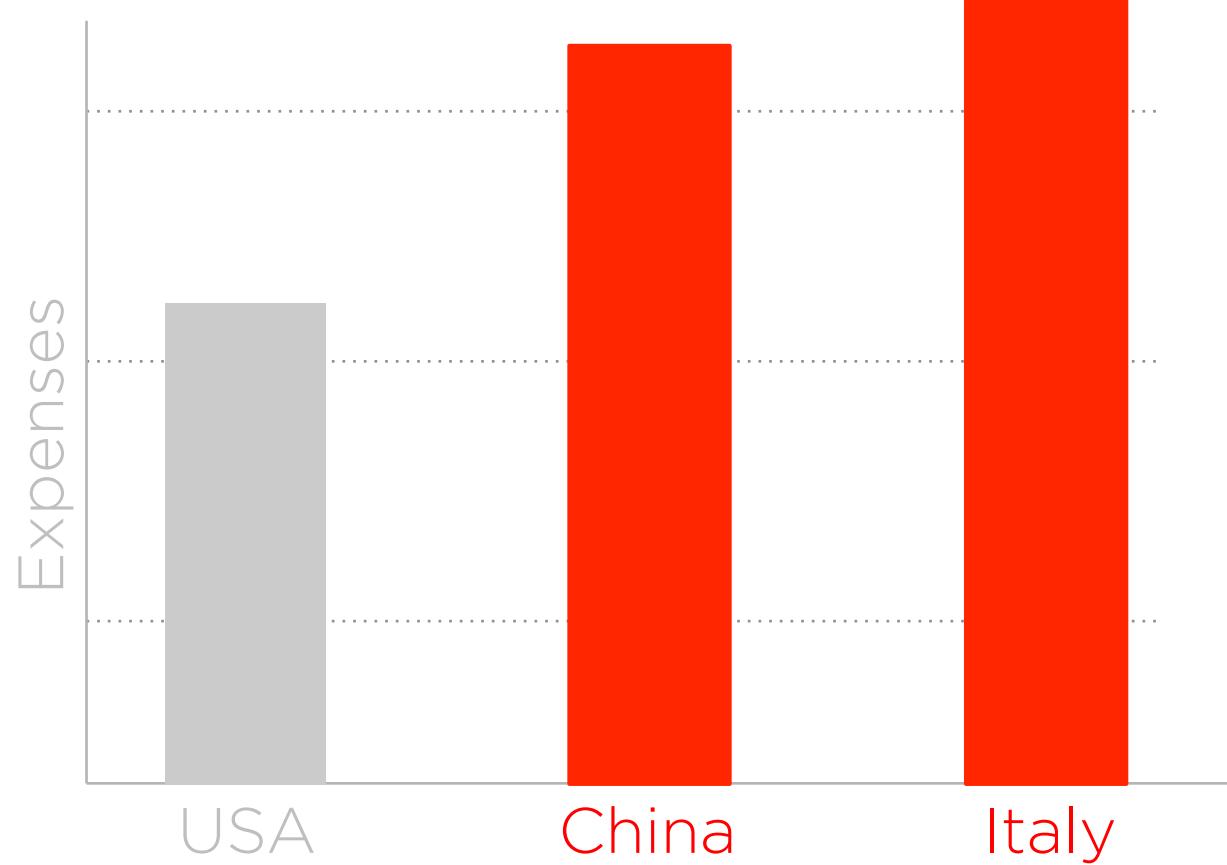
splunk>
POWERED

Table

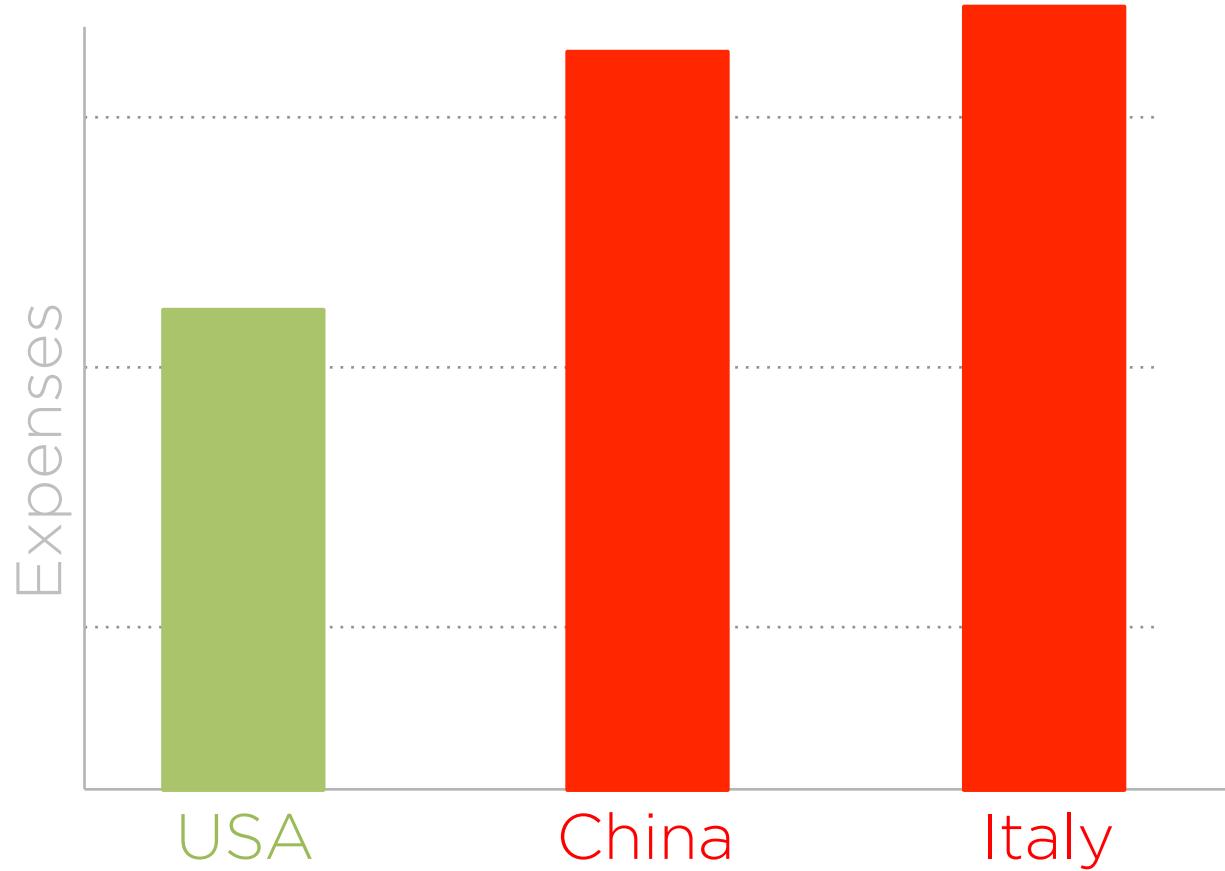




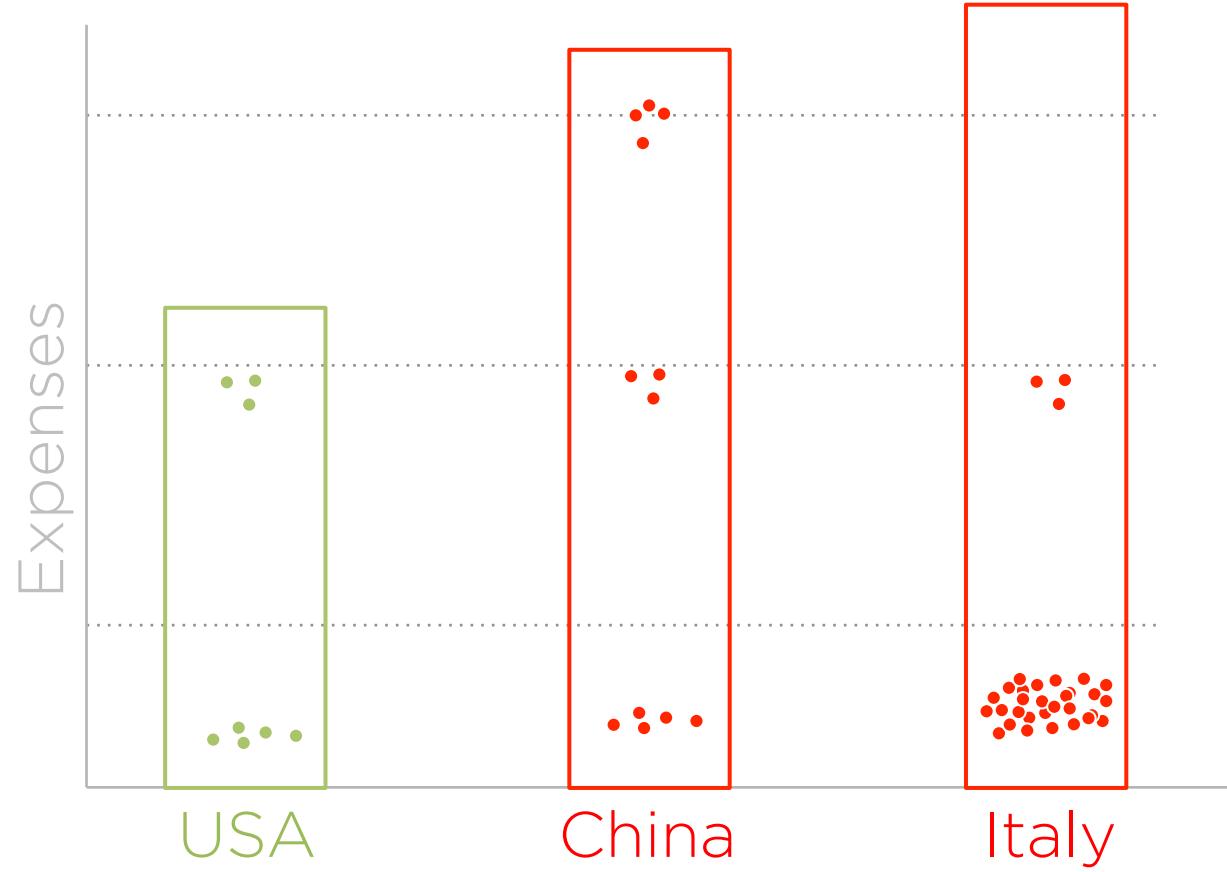
```
SELECT sum(cost)  
FROM expenses  
GROUPBY country
```



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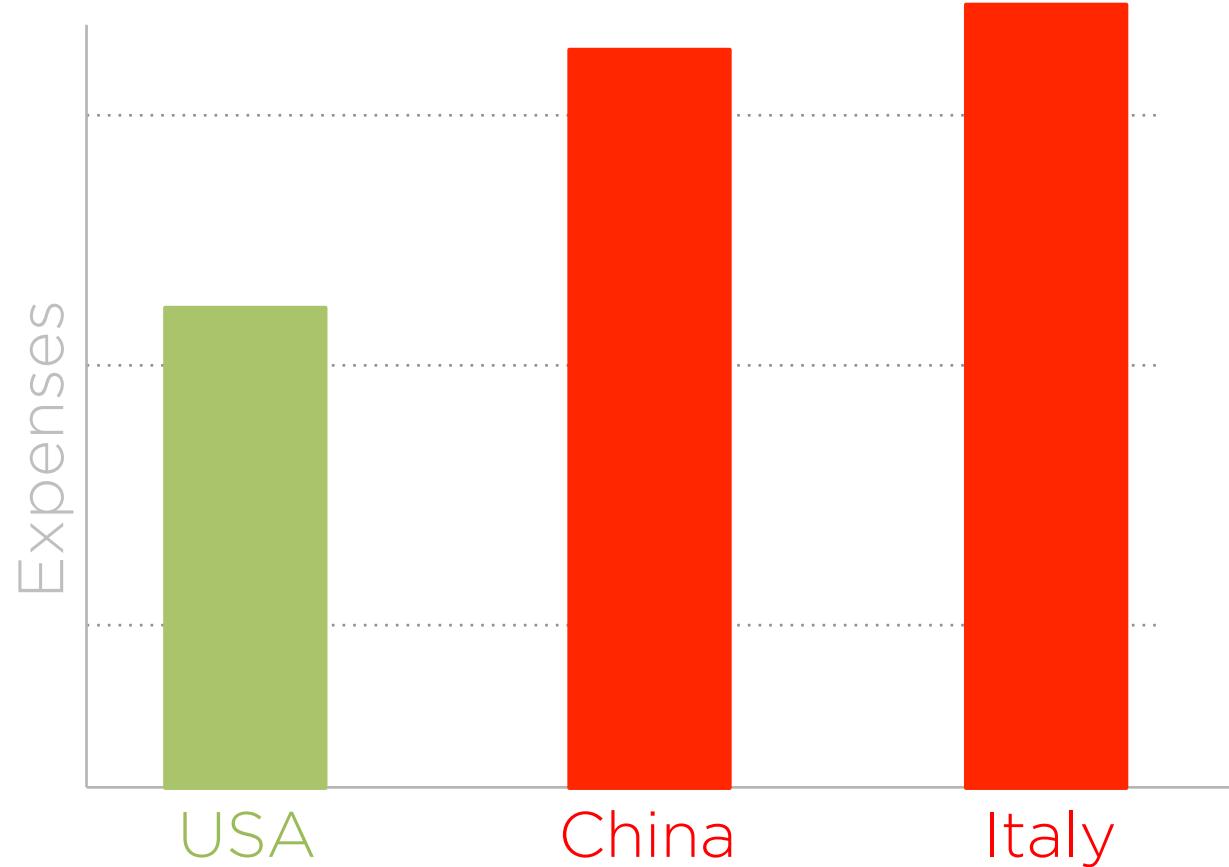


```
SELECT sum(cost)
FROM expenses
GROUPBY country
```

Given

Outlier and normal results

Understand Why



```
SELECT sum(cost)  
FROM expenses  
GROUPBY country
```

Given

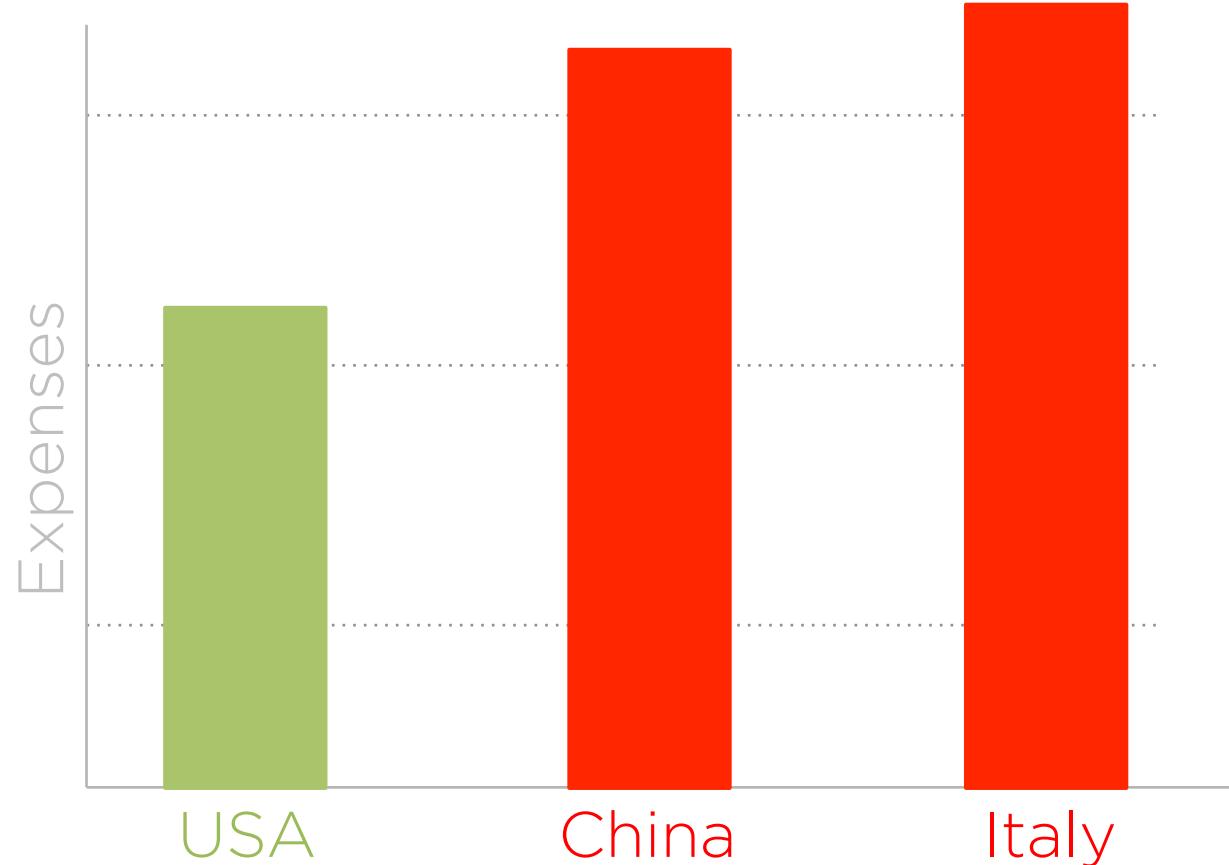
Outlier and normal results

What input properties

caused the outliers?

most caused the outliers?

caused outliers but didn't
affect normal outputs?

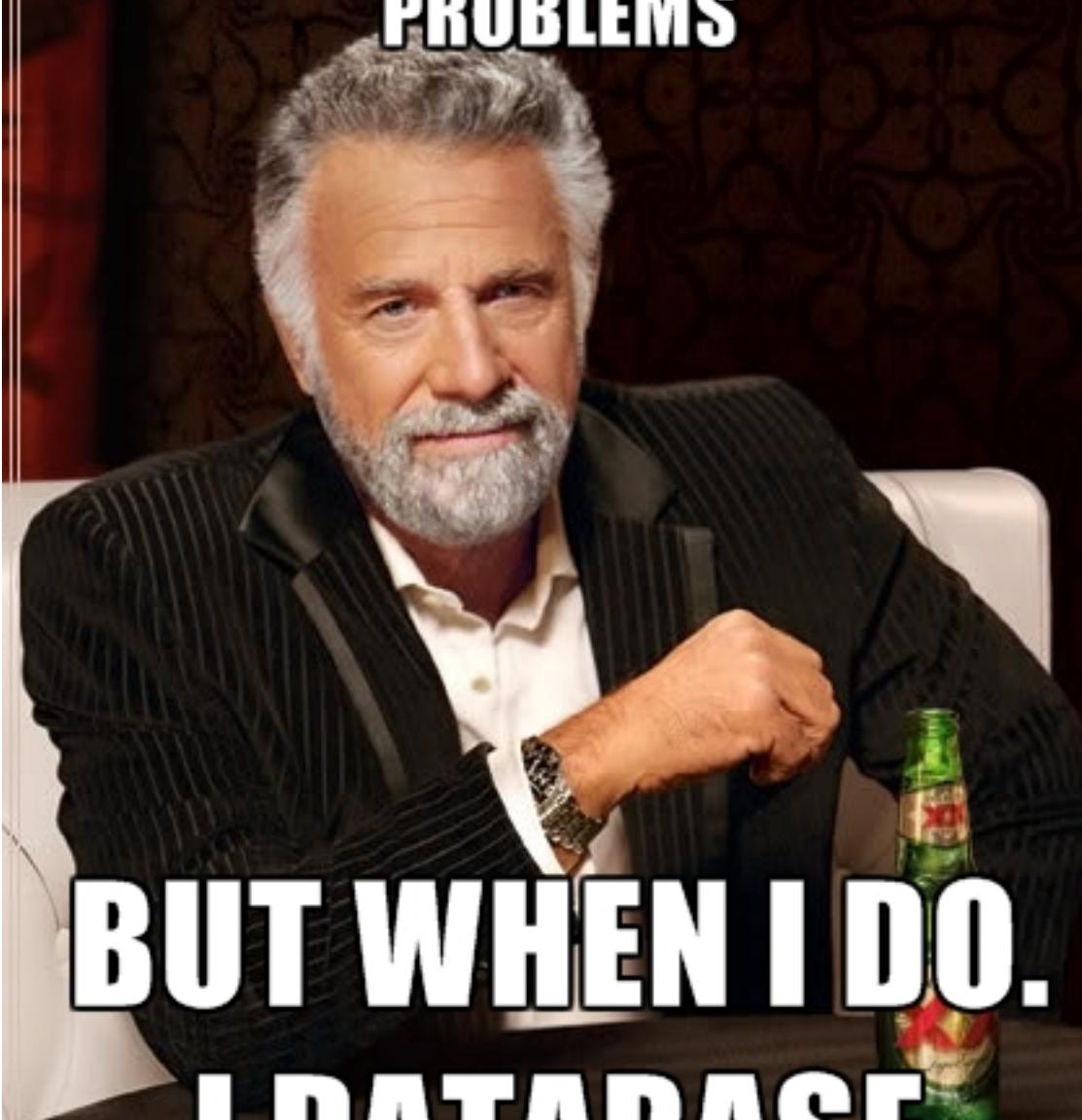


```
SELECT sum(cost)  
FROM expenses  
GROUPBY country
```

Can't Touch This



I DON'T ALWAYS SOLVE
PROBLEMS

A photograph of the character "The Most Interesting Man in the World" from the TV show "Granite City". He is a middle-aged man with a full, grey beard and mustache, wearing a dark pinstripe suit jacket over a white shirt. He is seated in a white armchair, looking directly at the camera with a slight smile. His right hand is resting on his lap, and his left hand is pointing towards a green bottle of Dos Equis beer on a wooden table in front of him.

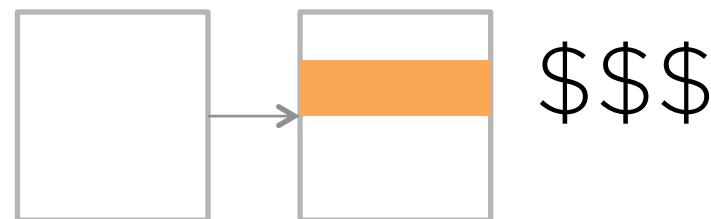
BUT WHEN I DO.
I DATABASE

Provenance



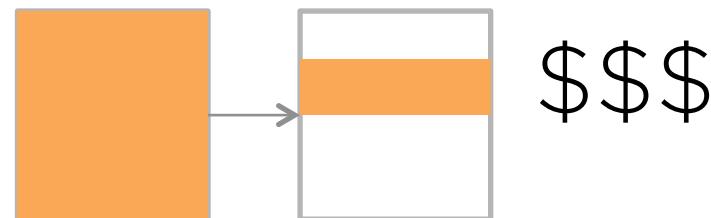
Provenance

SELECT SUM(cost)
FROM sam's bank account



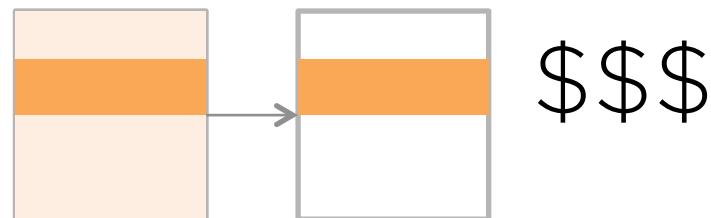
Provenance

SELECT SUM(cost)
FROM sam's bank account



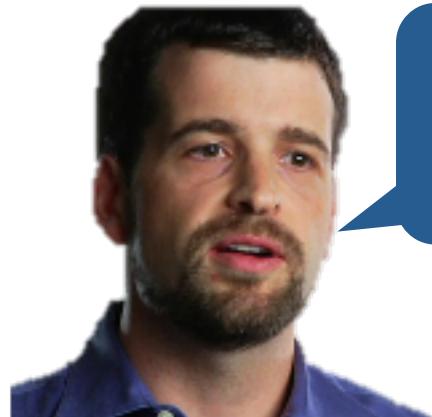
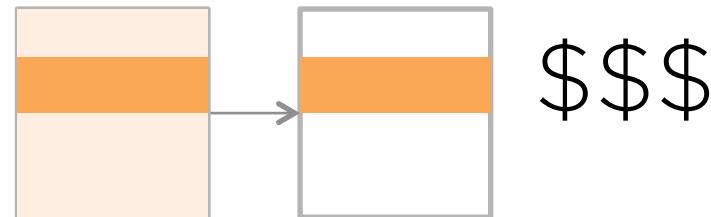
Provenance

```
SELECT SUM(cost)  
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Provenance

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SELECT SUM(cost)  
FROM sam's bank account
```



Proven

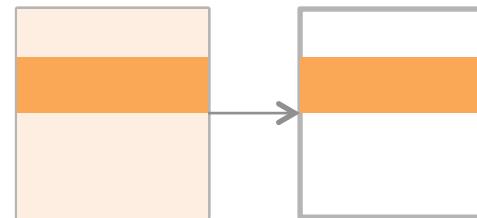
WHAT'S THE POINT



zipmeme

Provenance

SELECT SUM(cost)
FROM sam's bank account

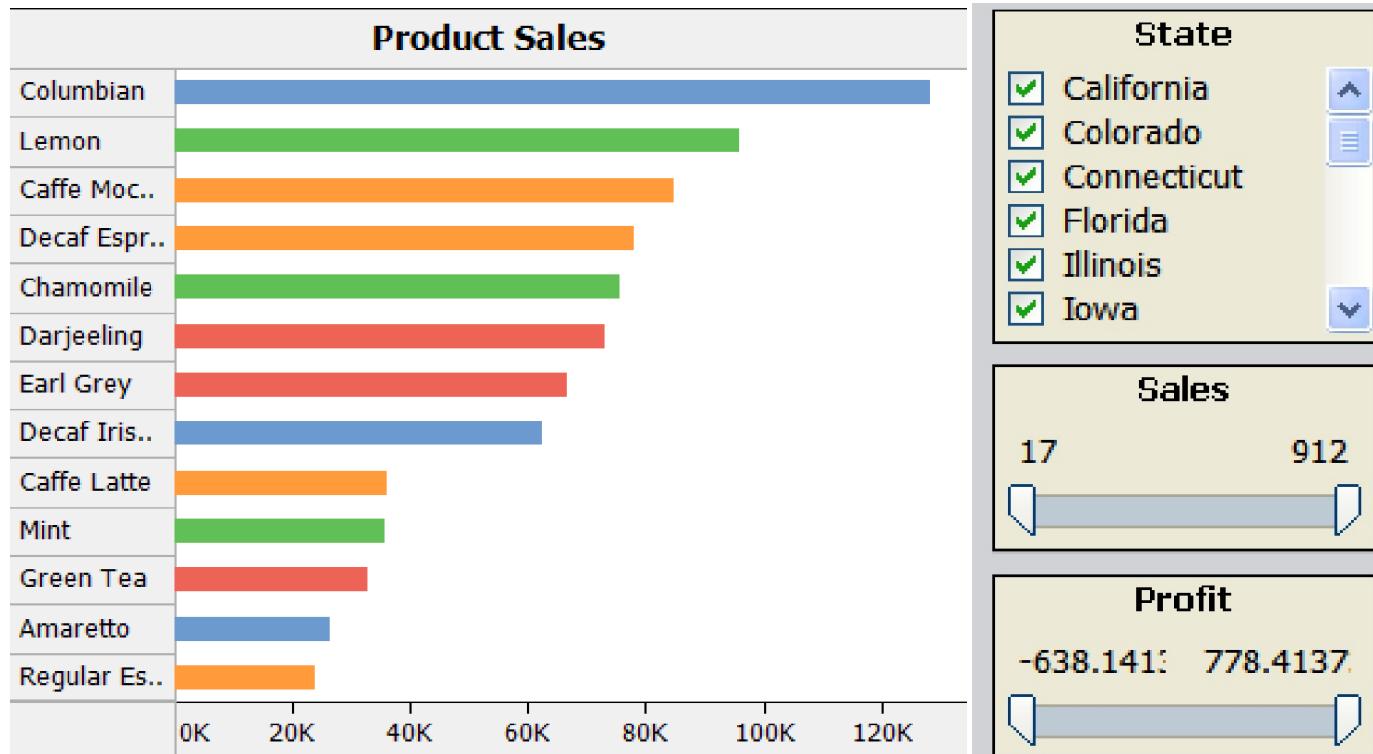


Filter for
“most influential”

~~Provenance~~

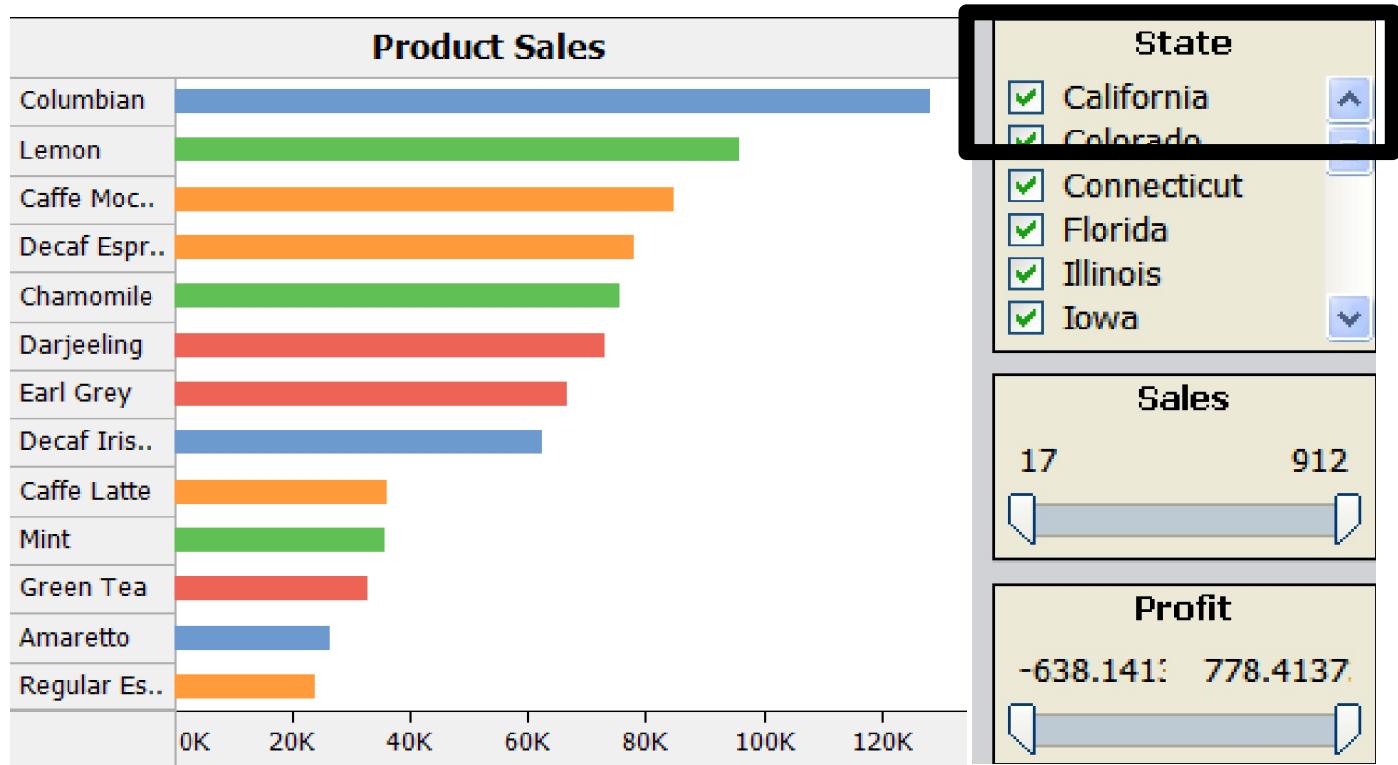


Provenance



Faceting

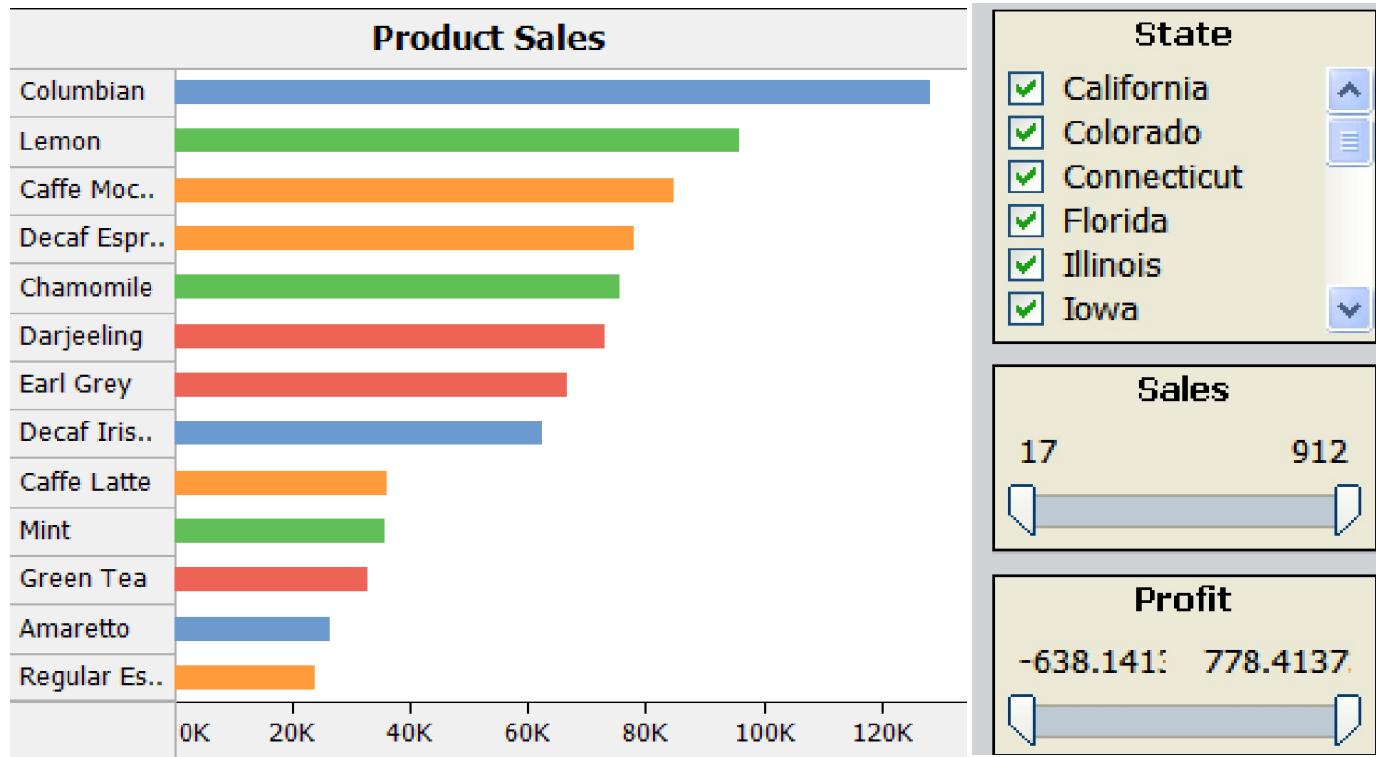
Provenance



Faceting

Provenance

Faceting



Dimensionality :(
Dealing with multiple outliers?

~~Provenance~~



~~Faceting~~

~~Provenance~~



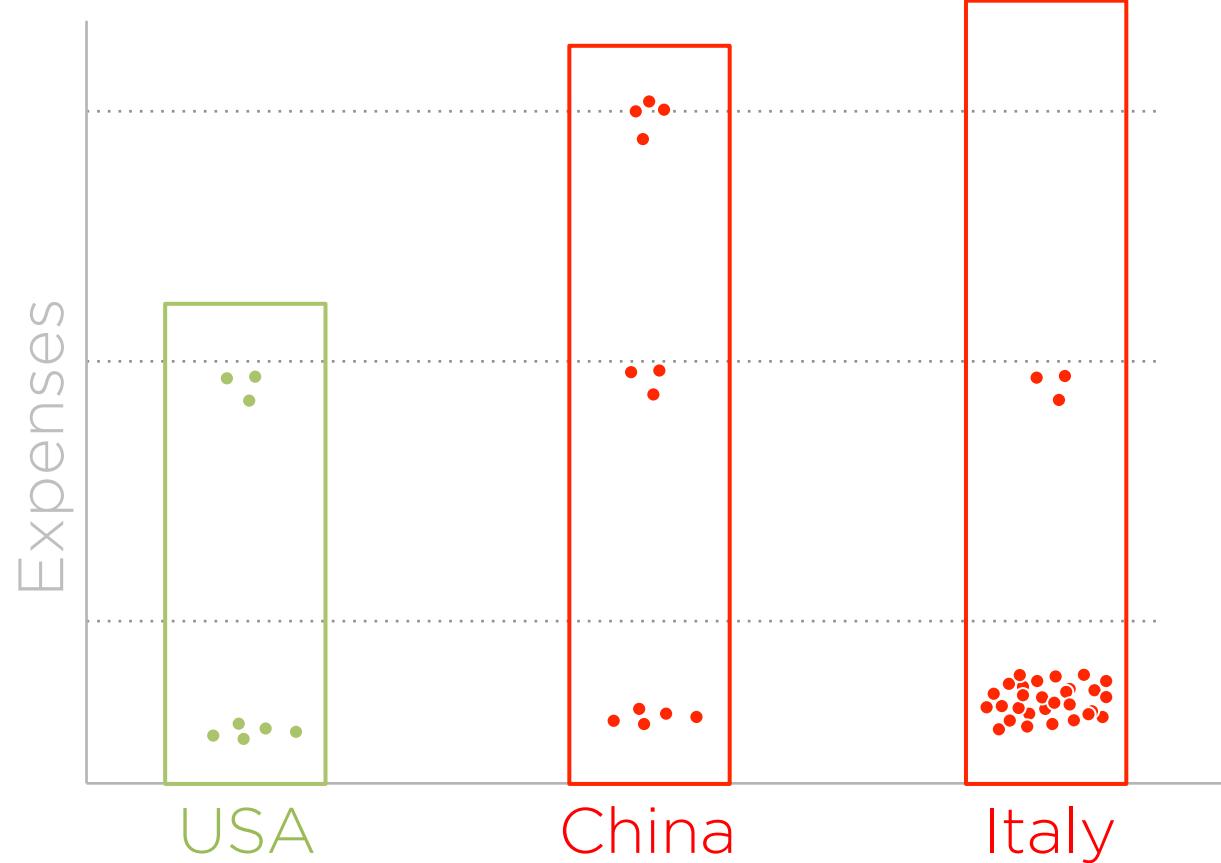
~~Faceting~~

Scorpion!

Given

Outlier and normal results

Understand Why

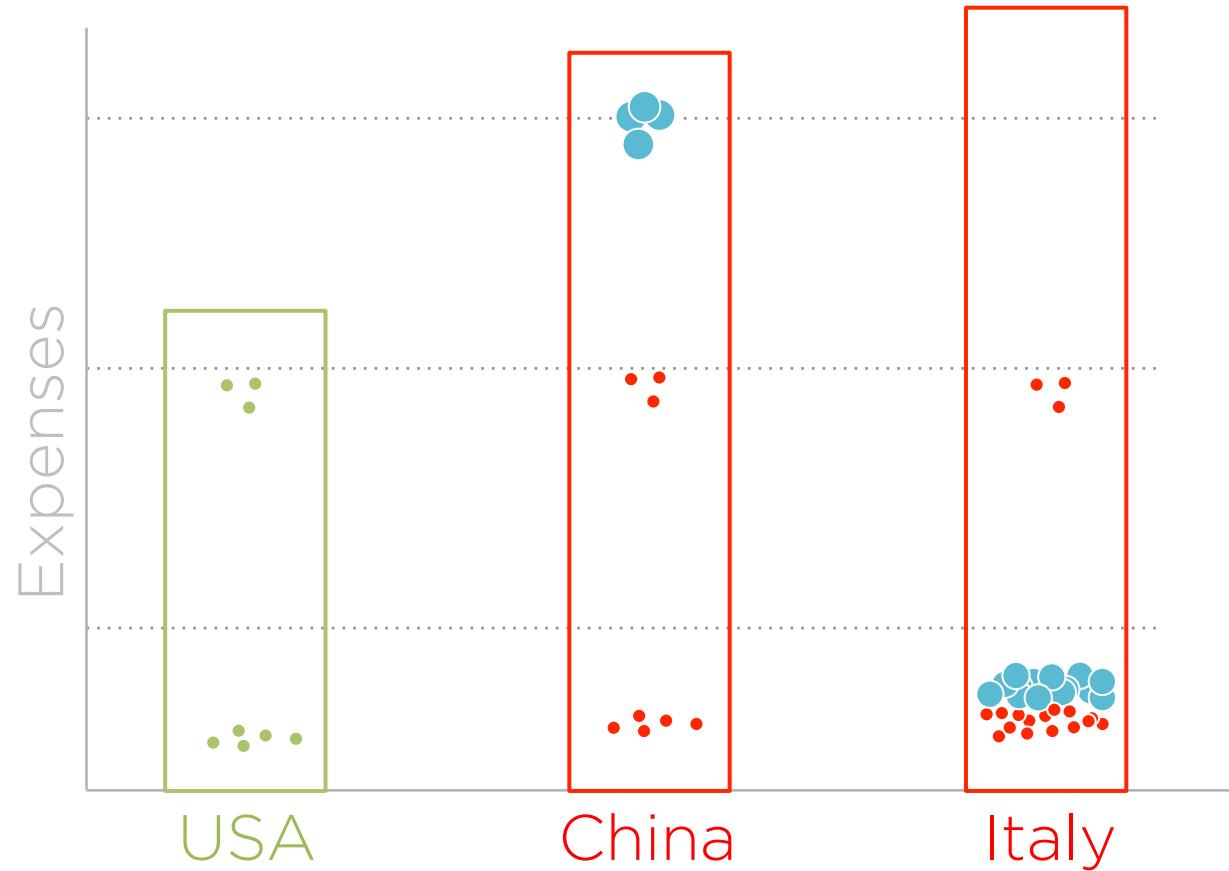


Given

Outlier and normal results

Find

Predicates correlated with outliers



Desc = "toilets"

Given

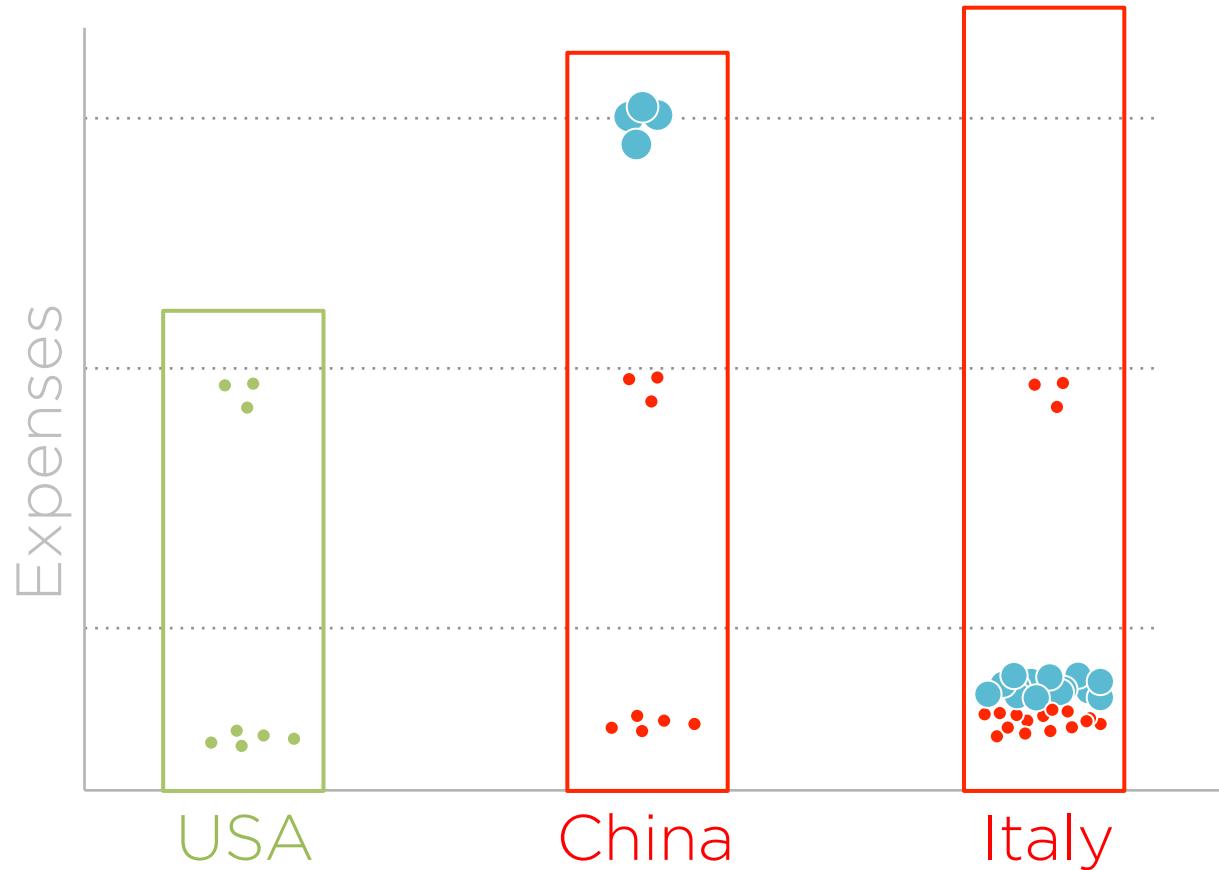
Outlier and normal results

Find

Predicates correlated with outliers

s.t.

Removing predicate from inputs “fixes” outliers & maintains normal results



Desc = “toilets”

Given

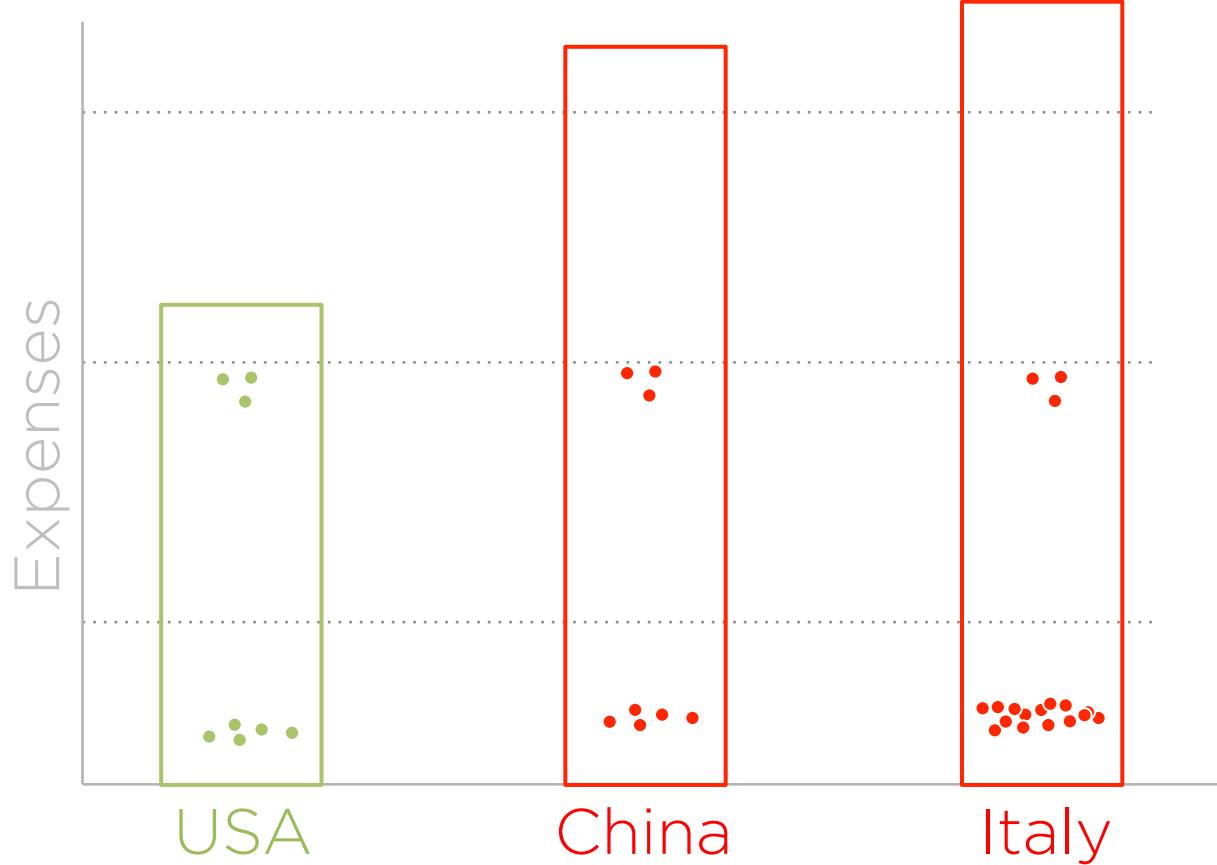
Outlier and normal results

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Removing predicate from inputs “fixes” outliers & maintains normal results



~~Dese = “toilets”~~

Given

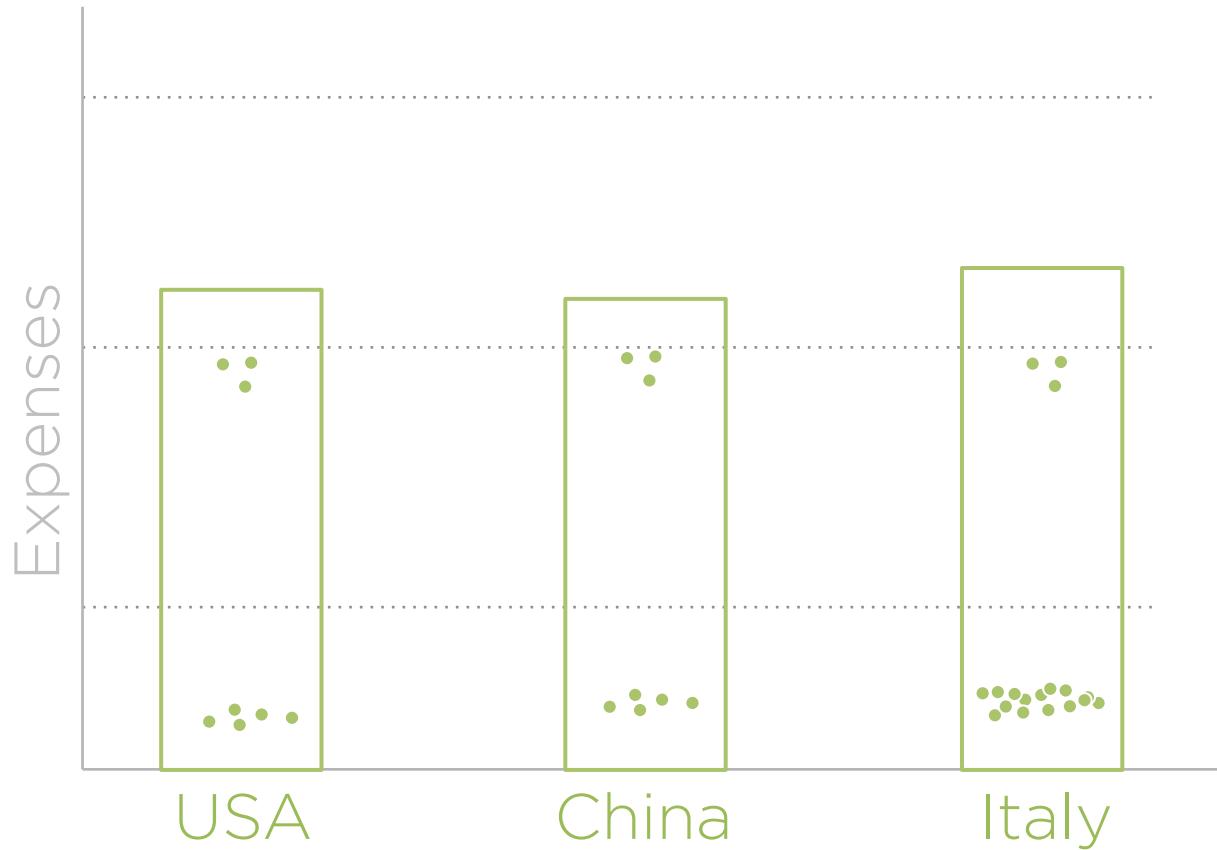
Outlier and normal results

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Predicates correlated with outliers

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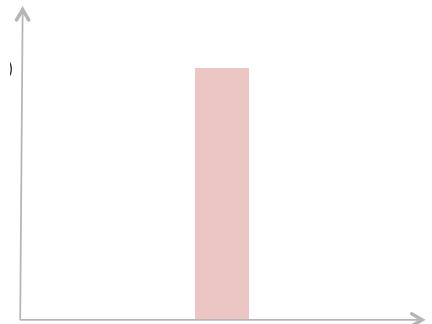
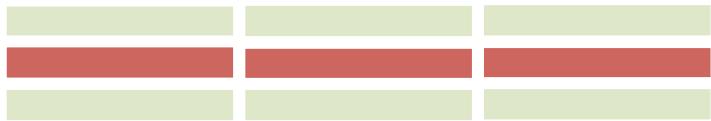
~~Dese = “toilets”~~

Formalize “influence” as metric

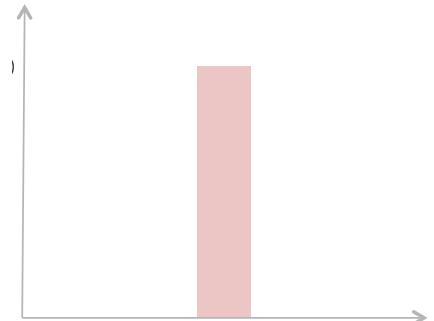
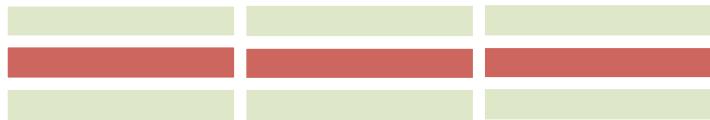
Predicate search heuristics

Some results

T



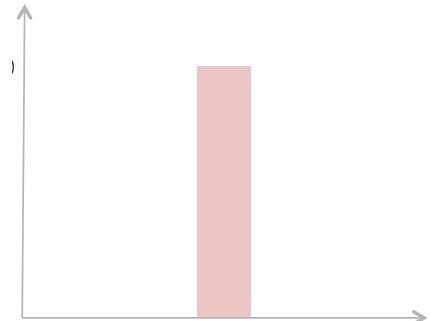
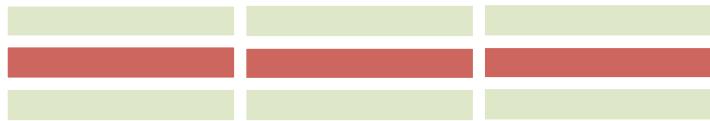
T



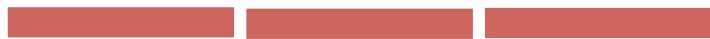
p

Desc = "toilet"

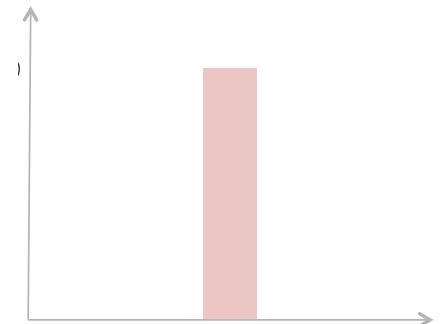
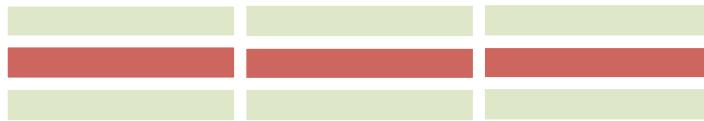
T



p(T)



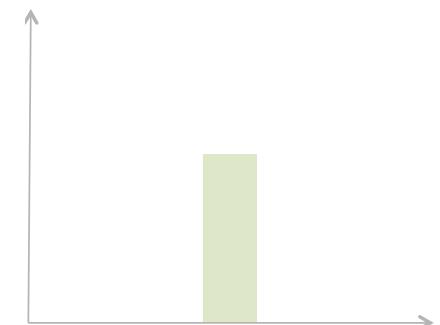
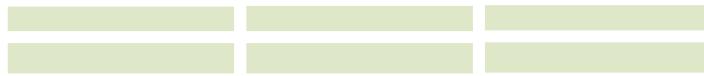
T

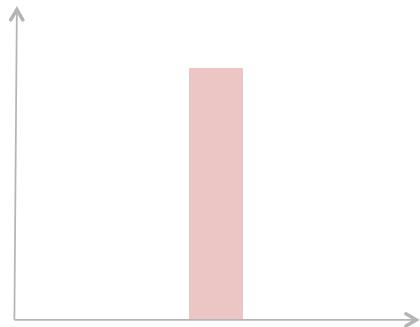


p(T)

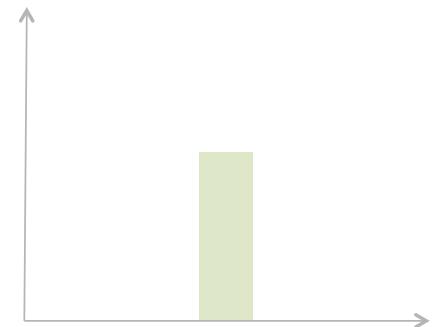


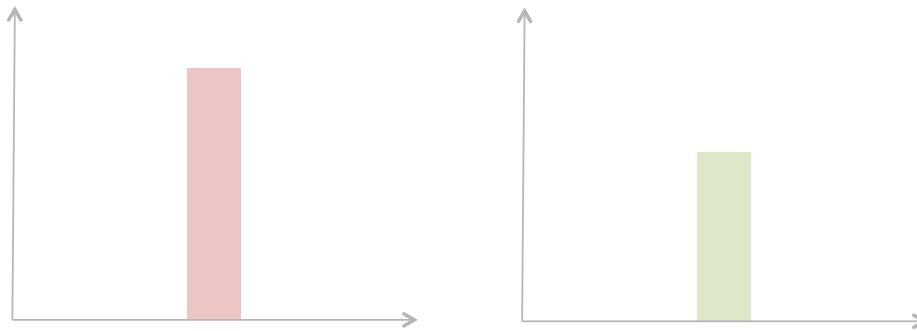
T - p(T)



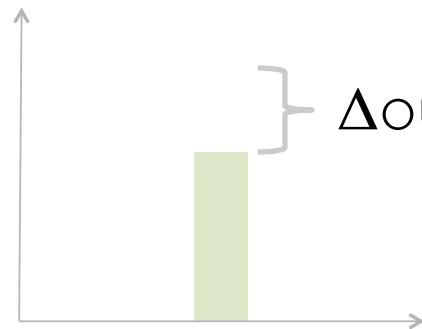
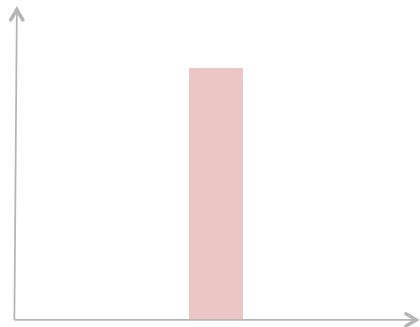


$p(T)$ ■ ■ ■

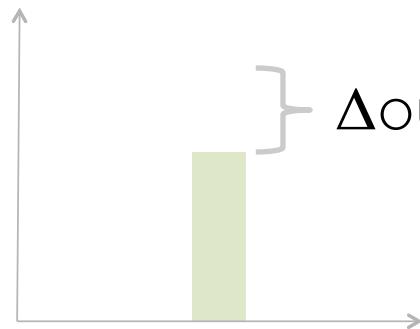
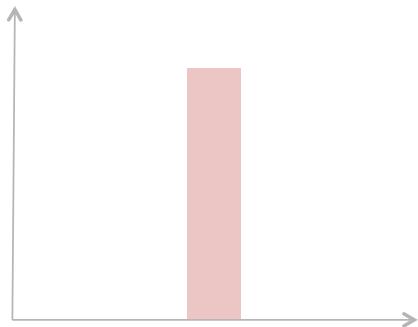




$p(T)$ ■ ■ ■



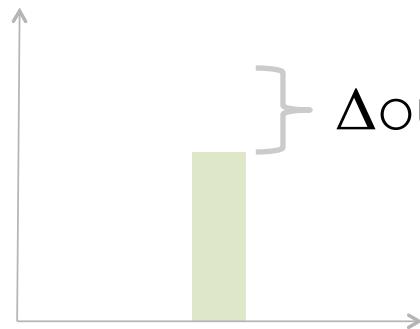
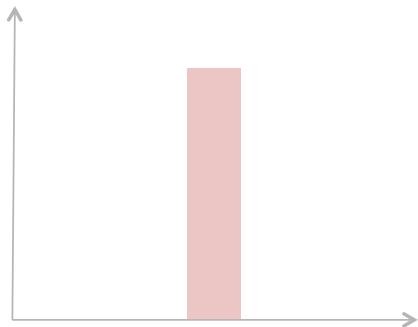
$p(T)$ Three horizontal red bars of equal length are shown side-by-side, representing the components of the probability distribution $p(T)$.



$p(T)$



$\} |p(T)|$



$p(T)$



$\} |p(T)|$

$$\frac{\Delta\text{output}}{|p(T)|}$$

**Influence
Metric**

$$\frac{\Delta f(x)}{\Delta x}$$

**Sensitivity
Analysis**

$$\frac{\Delta \text{output}}{|p(T)|}$$

**Influence
Metric**

Δ Output

$$\frac{\Delta \text{output}}{|p(T)|}$$

“High vs Low”

$|p(T)|$

Δ Normal

Multiple Outputs

Δ Output

$$\frac{\Delta \text{output}}{|p(T)|}$$

“High vs Low”

$$\frac{\Delta \text{output} \cdot V}{|p(T)|}$$

$|p(T)|$

Δ Normal

Multiple Outputs

Δ Output

$$\frac{\Delta \text{output}}{|p(T)|}$$

“High vs Low”

$$\frac{\Delta \text{output} \cdot V}{|p(T)|}$$

$|p(T)|$

$$\frac{\Delta \text{output} \cdot V}{|p(T)|^c}$$

Δ Normal

Multiple Outputs

Δ Output

$$\frac{\Delta \text{Output}}{|p(T)|}$$

“High vs Low”

$$\frac{\Delta \text{Output} \cdot V}{|p(T)|}$$

$|p(T)|$

$$\frac{\Delta \text{Output} \cdot V}{|p(T)|^c}$$

Δ Normal

$$\frac{\Delta \text{outlier} \cdot V}{|p(T)|^c} - |\Delta \text{Normal}|$$

Multiple Outputs

Δ Output

$$\frac{\Delta \text{output}}{|p(T)|}$$

“High vs Low”

$$\frac{\Delta \text{output} \cdot V}{|p(T)|}$$

$|p(T)|$

$$\frac{\Delta \text{output} \cdot V}{|p(T)|^c}$$

Δ Normal

$$\frac{\Delta \text{outlier} \cdot V}{|p(T)|^c} - |\Delta \text{Normal}|$$

Multiple Outputs

$$\text{mean}_{\text{outlier}} \frac{\Delta \text{outlier} \cdot V}{|p(T)|^c} - \max_{\text{normal}} |\Delta \text{Normal}|$$

Δ output

$$\frac{\Delta_{\text{outlier}}}{|P(T)|}$$

“High vs Low”

$$\frac{\Delta_{\text{outlier}} \cdot V}{|P(T)|}$$

influence(p)

Δ Normal

$$\frac{\Delta_{\text{outlier}} \cdot V}{|P(T)|^c} - |\Delta_{\text{Hold-out}}|$$

Multiple Outputs

$$\text{mean}_{\text{outlier}} \frac{\Delta_{\text{outlier}} \cdot V}{|P(T)|^c} - \max_{\text{normal}} |\Delta_{\text{Hold-out}}|$$

Formalize “influence” as metric

Predicate search heuristics

Some results

$$p^* = \operatorname{argmax}_{p \in \text{predicates}} \text{influence}(p)$$

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$$\mathcal{O}(\text{agg}(T-p(T)))$$

$$\text{SUM}(\{1,2,3,4,5\}) = 15$$

$$p^* = \operatorname{argmax}_{p \in \text{predicates}} \text{influence}(p)$$


$$\mathcal{O}(\text{agg}(T-p(T)))$$

$$\text{SUM}(\{1, 2, 3, \overbrace{4, 5}\}) = 15$$

$$p^* = \operatorname{argmax}_{p \in \text{predicates}} \text{influence}(p)$$

$\overbrace{\quad\quad\quad}$
 $O(\text{agg}(T-p(T)))$

$$\begin{array}{c} p \\ \text{SUM}(\{1,2,\underline{3},\cancel{4},\cancel{5}\}) = 15 \\ \{4,5\} \end{array}$$

$$p^* = \operatorname{argmax}_{p \in \text{predicates}} \text{influence}(p)$$

$\overbrace{\quad\quad\quad}^{\mathcal{O}(\text{agg}(T-p(T)))}$

$$\begin{array}{r} p \\ \overbrace{\text{SUM}(\{1,2,3,\cancel{4,5}\}) = 15}^{\cancel{4,5}} \\ - \\ \{4,5\} \\ \overbrace{\text{SUM}(\{1,2,3\})}^{} = 6 \end{array}$$

$$p^* = \operatorname{argmax}_{p \in \text{predicates}} \text{influence}(p)$$

$$\mathcal{O}(\text{agg}(\mathcal{T}-p(\mathcal{T})))$$

$$p^* = \operatorname{argmax}_{p \in \text{predicates}} \text{influence}(p)$$

$$\overbrace{\quad\quad\quad}^{\mathcal{O}(\text{exponential})} \quad \overbrace{\quad\quad\quad}^{\mathcal{O}(\text{agg}(T-p(T)))}$$

Operator Properties

$$p^* = \operatorname{argmax}_{p \in \text{predicates}} \text{influence}(p)$$

$$\underbrace{\qquad\qquad\qquad}_{O(\text{exponential})} \qquad \underbrace{\qquad\qquad\qquad}_{O(\text{agg}(T-p(T)))}$$

Operator Properties

$$p^* = \operatorname{argmax}_{p \in \text{predicates}} \text{influence}(p)$$

$O(\text{exponential})$ $O(\text{agg}(p(T)))$

**Incrementally
removable**

$$\text{SUM}(\{1, 2, 3, \overbrace{4, 5}\}) = 15$$

$$p^* = \operatorname{argmax}_{p \in \text{predicates}} \text{influence}(p)$$

$$\overbrace{\quad\quad\quad}^{O(\text{exponential})} \quad \overbrace{\quad\quad\quad}^{O(\text{agg}(p(T)))}$$

**Incrementally
removable**

$$\begin{aligned} p \\ \text{SUM}(\{1,2,3,\overbrace{4,5}\}) &= 15 \\ 15 - \text{SUM}(\{4,5\}) &= 6 \end{aligned}$$

$$p^* = \operatorname{argmax}_{p \in \text{predicates}} \text{influence}(p)$$

$$\underbrace{\quad}_{O(\text{exponential})} \quad \underbrace{\quad}_{O(\text{agg}(p(T)))}$$

**Incrementally
removable**

SUM
COUNT
AVG
STDDEV

$$p^* = \operatorname{argmax}_{p \in \text{predicates}} \text{influence}(p)$$

$$\underbrace{\qquad\qquad\qquad}_{O(\text{exponential})} \qquad \underbrace{\qquad\qquad\qquad}_{O(\text{agg}(p(T)))}$$

Incrementally
removable

MEDIAN

MODE

SUM
COUNT
AVG
STDDEV

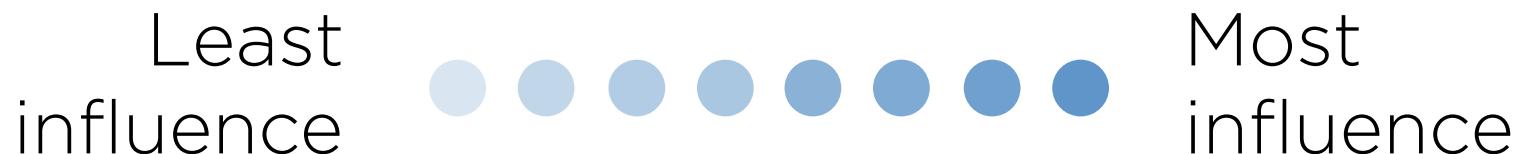
$$p^* = \operatorname{argmax}_{p \in \text{predicates}}$$

influence(p)

O(exponential)

O(agg(p(T)))

Incrementally
removable

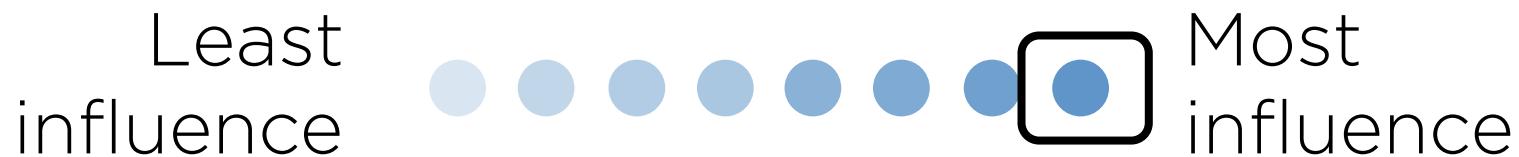


$$p^* = \operatorname{argmax}_{p \in \text{predicates}} \text{influence}(p)$$

$O(\text{exponential})$ $O(\text{agg}(p(T)))$

Independent

Incrementally removable

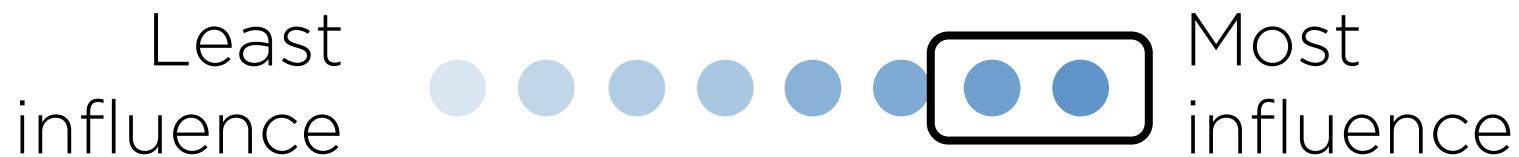


$$p^* = \operatorname{argmax}_{p \in \text{predicates}} \text{influence}(p)$$

O(exponential) O(agg(p(T)))

Independent

Incrementally
removable

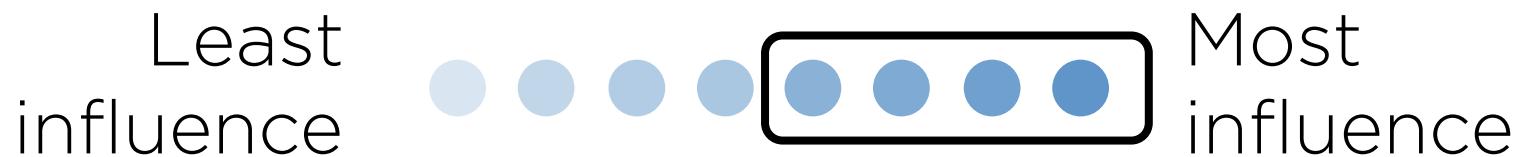


$$p^* = \operatorname{argmax}_{p \in \text{predicates}} \text{influence}(p)$$

$O(\text{exponential})$ $O(\text{agg}(p(T)))$

Independent

Incrementally removable



$$p^* = \operatorname{argmax}_{p \in \text{predicates}} \text{influence}(p)$$

$O(\text{exponential})$ $O(\text{agg}(p(T)))$

Independent

**Incrementally
removable**



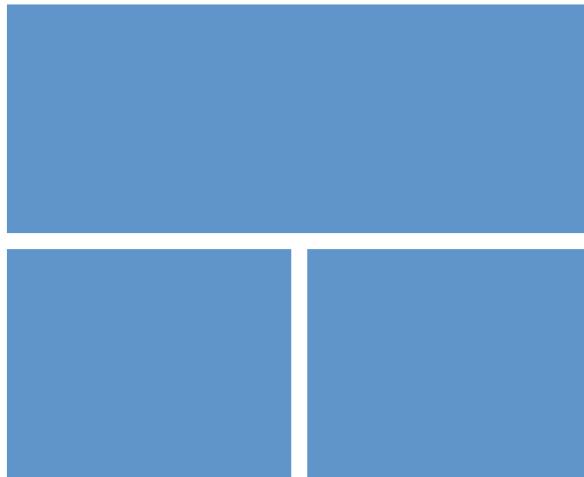
$$p^* = \operatorname{argmax}_{p \in \text{predicates}} \text{influence}(p)$$

$$\overbrace{\quad\quad\quad}^{O(\text{exponential})} \quad \overbrace{\quad\quad\quad}^{O(\text{agg}(p(T)))}$$

Top Down

Independent

**Incrementally
removable**



$$p^* = \operatorname{argmax}_{p \in \text{predicates}} \text{influence}(p)$$

$O(\text{exponential})$ $O(\text{agg}(p(T)))$

Top Down

Independent

Incrementally removable



$$p^* = \operatorname{argmax}_{p \in \text{predicates}} \text{influence}(p)$$

$O(\text{exponential})$ $O(\text{agg}(p(T)))$

Top Down

Independent

Incrementally removable



$$p^* = \operatorname{argmax}_{p \in \text{predicates}} \text{influence}(p)$$

$O(\text{exponential})$ $O(\text{agg}(p(T)))$

Top Down

Independent

Incrementally removable

Top Down

$$p^* = \operatorname{argmax}_{p \in \text{predicates}} \text{influence}(p)$$

$O(\text{exponential})$

Independent

Anti-monotonic

$O(\text{agg}(p(T)))$

Incrementally removable

$p' \subset p$

$$p^* = \operatorname{argmax}_{p \in \text{predicates}} \text{influence}(p)$$

$$\overbrace{\quad\quad\quad}^{O(\text{exponential})} \quad \overbrace{\quad\quad\quad}^{O(\text{agg}(p(T)))}$$

Top Down

Independent

**Incrementally
removable**

Anti-monotonic

$p' \subset p$  $\text{influence}(p') \leq \text{influence}(p)$

$$p^* = \underset{p \in \text{predicates}}{\operatorname{argmax}} \text{influence}(p)$$

$$\overbrace{\quad\quad\quad}^{\mathcal{O}(\text{exponential})} \quad \overbrace{\quad\quad\quad}^{\mathcal{O}(\text{agg}(p(T)))}$$

Top Down

Independent

Incrementally removable

Anti-monotonic



Top Down
Bottom Up

$$p^* = \operatorname{argmax}_{p \in \text{predicates}}$$

O(exponential)

Independent
Anti-monotonic

influence(p)

O(agg(p(T)))

**Incrementally
removable**



Top Down
Bottom Up

$$p^* = \operatorname{argmax}_{p \in \text{predicates}}$$

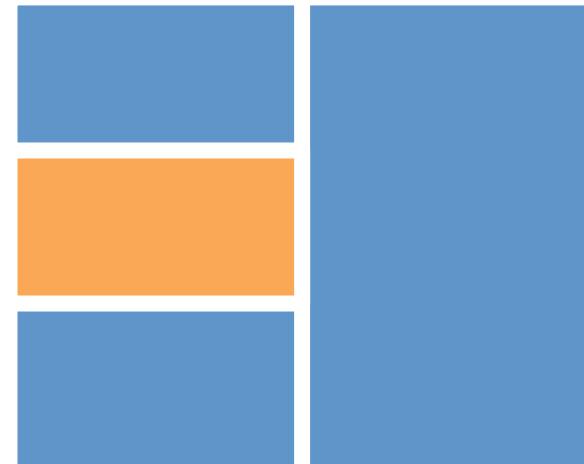
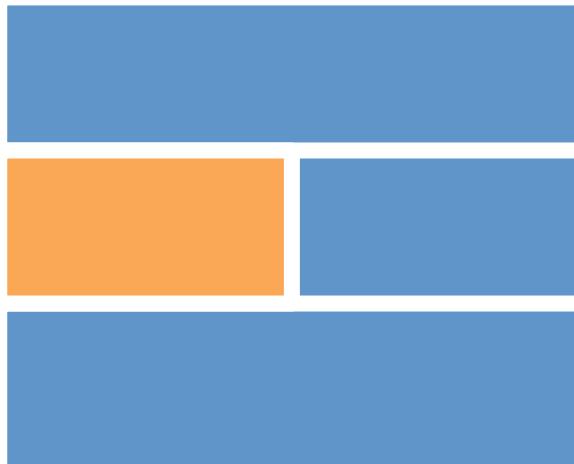
O(exponential)

Independent
Anti-monotonic

influence(p)

O(agg(p(T)))

**Incrementally
removable**



Top Down
Bottom Up

$$p^* = \operatorname{argmax}_{p \in \text{predicates}}$$

O(exponential)

Independent
Anti-monotonic

$\operatorname{influence}(p)$

O(agg($p(T)$))

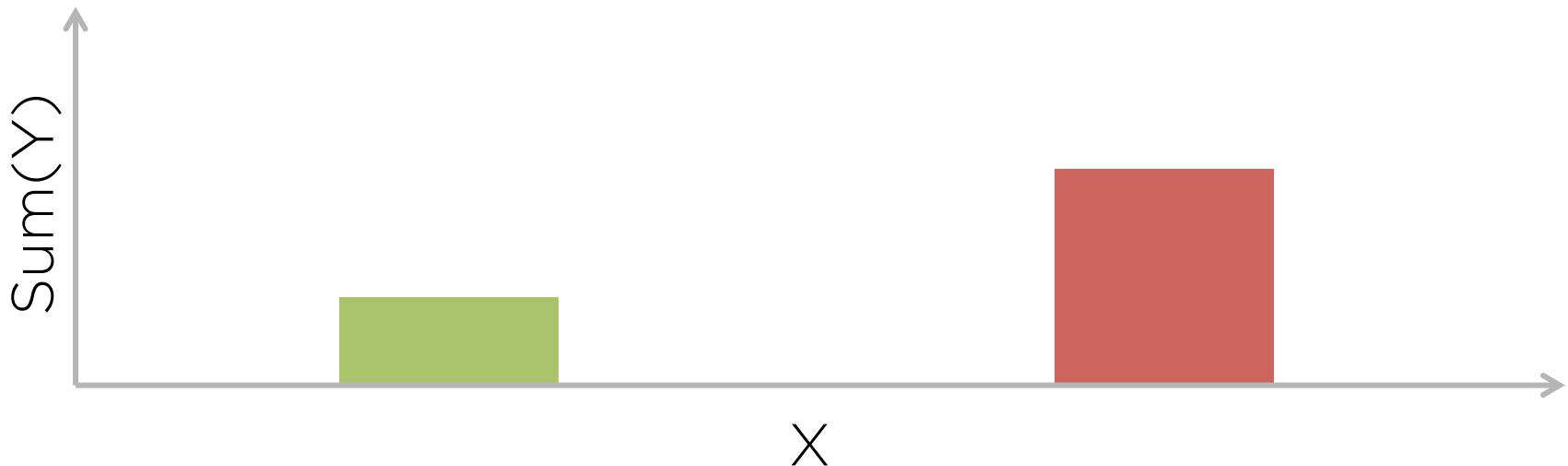
**Incrementally
removable**

Formalize “influence” as metric

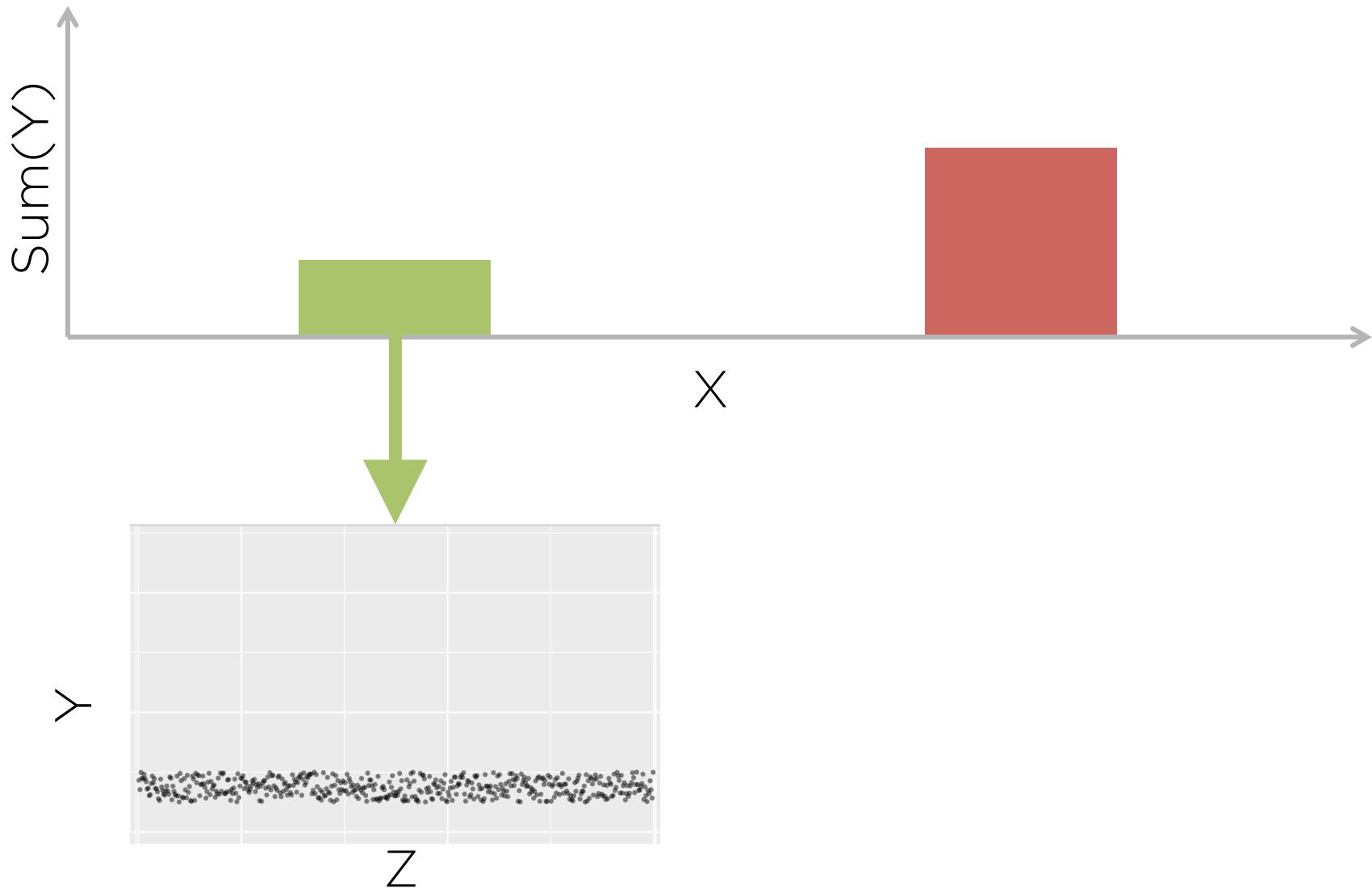
Predicate search heuristics

Some results

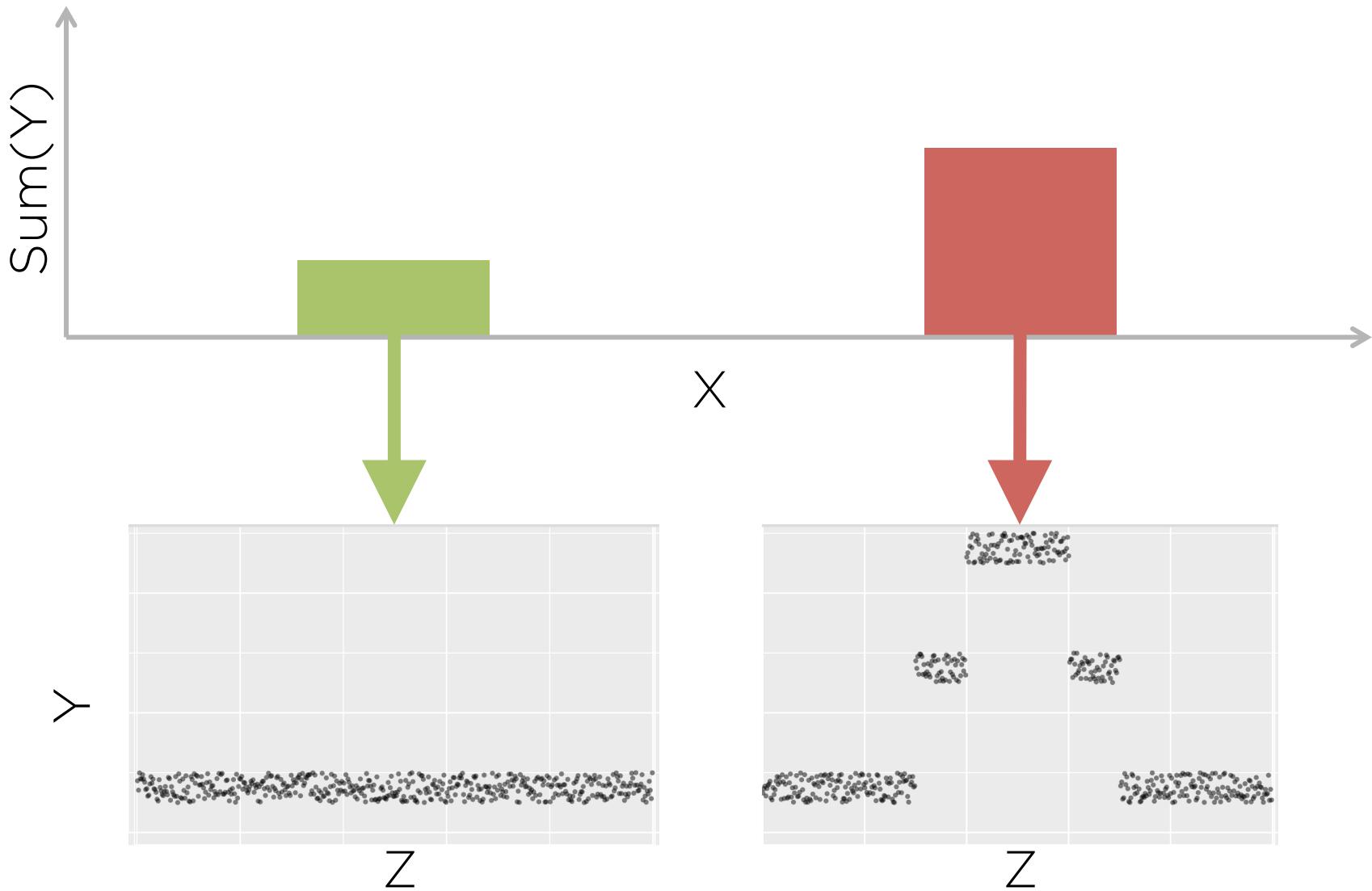
SELECT sum(Y) GROUPBY X



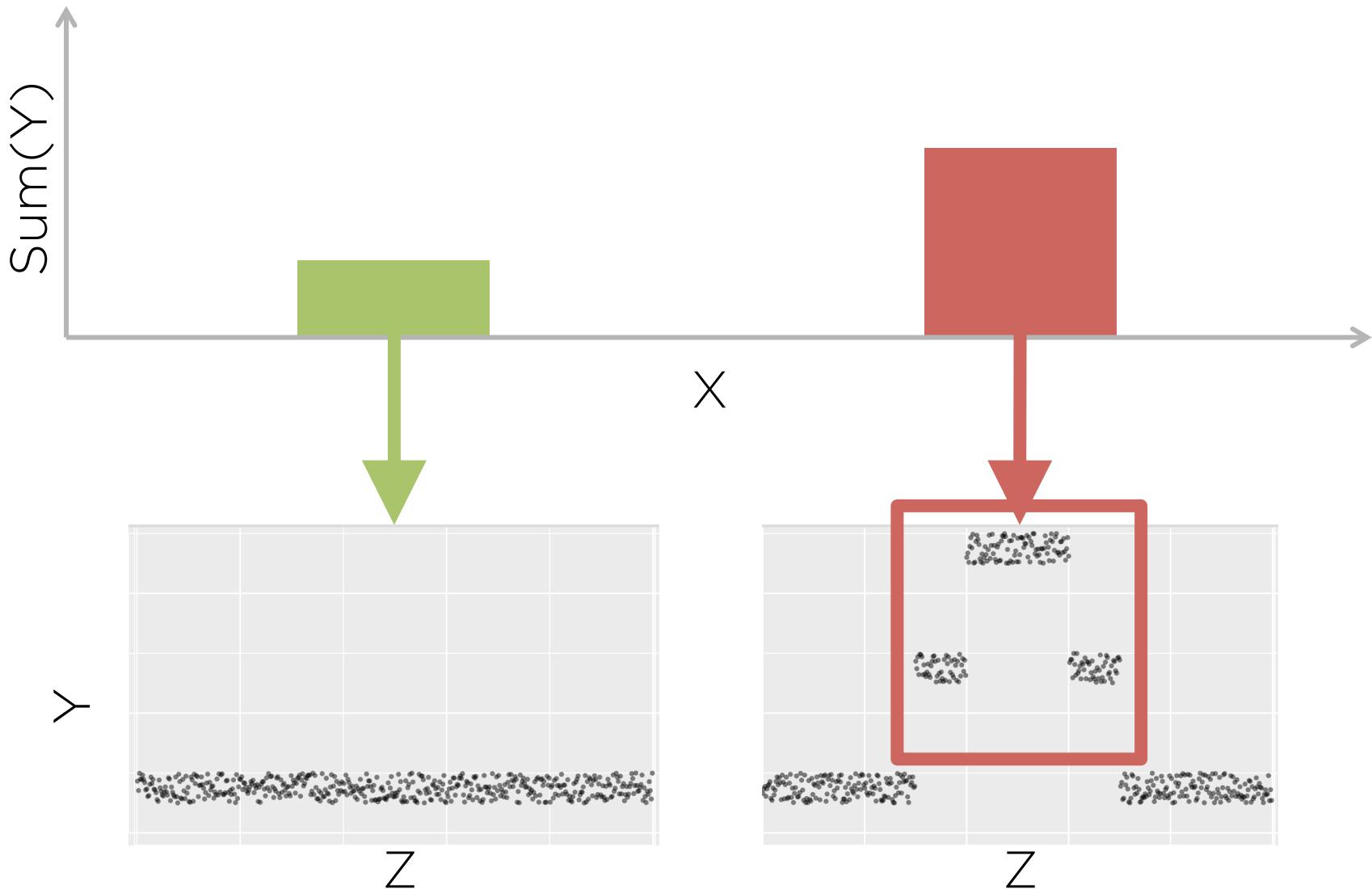
SELECT sum(Y) GROUPBY X



`SELECT sum(Y) GROUPBY X`



`SELECT sum(Y) GROUPBY X`

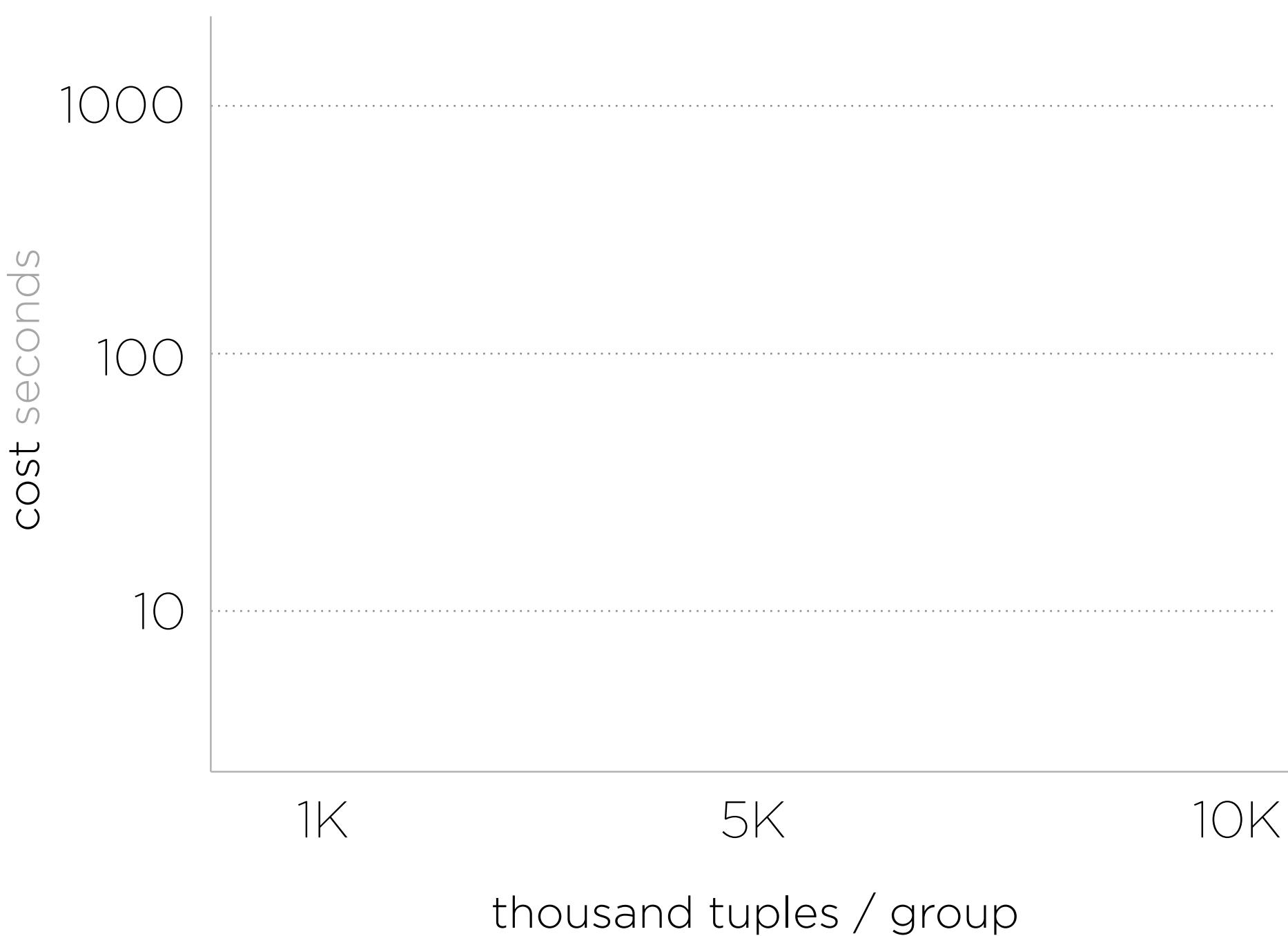


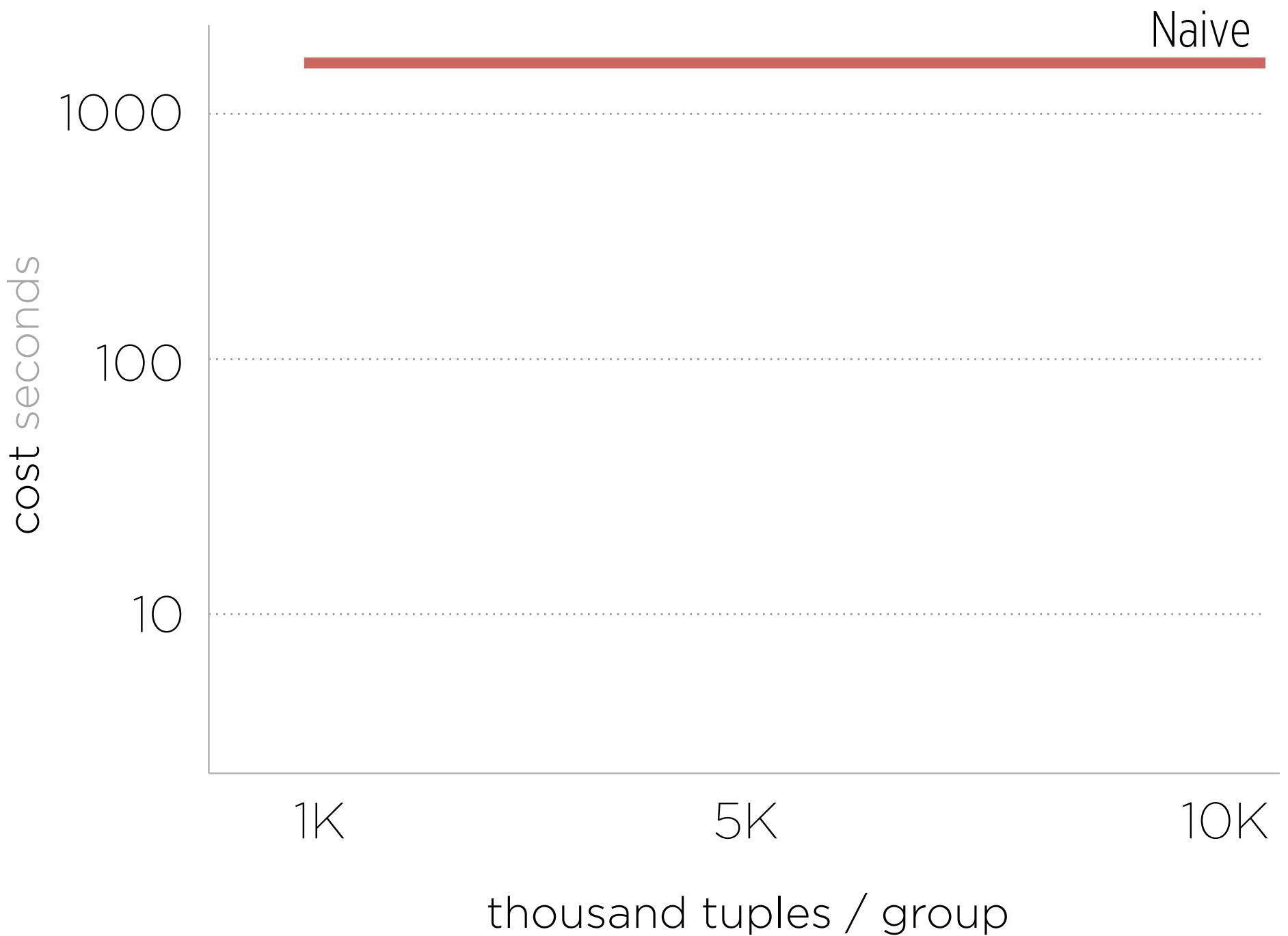
1K

5K

10K

thousand tuples / group





cost seconds

1000

100

10

Naive

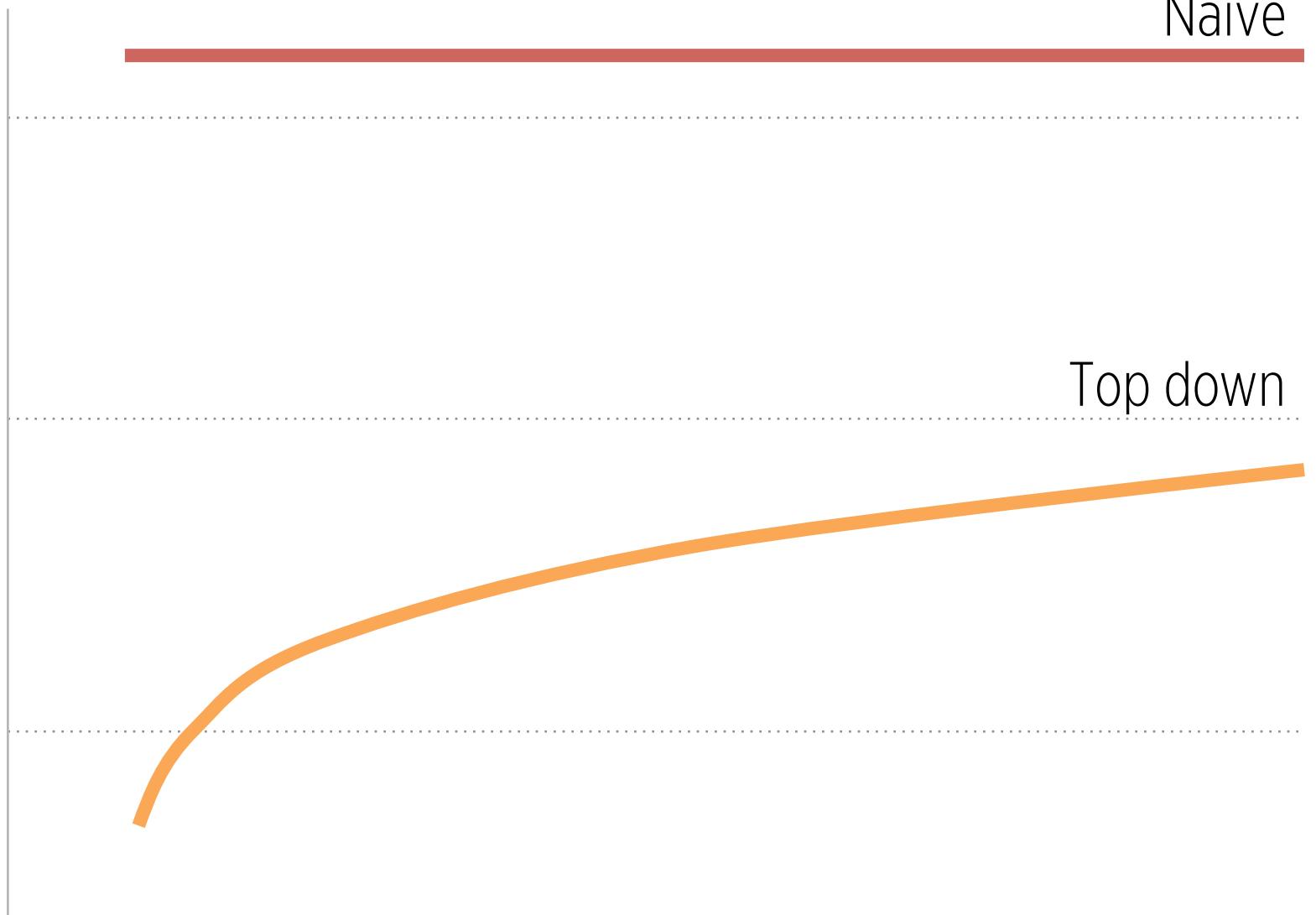
Top down

1K

5K

10K

thousand tuples / group



cost seconds

1000

100

10

Naive

Top down

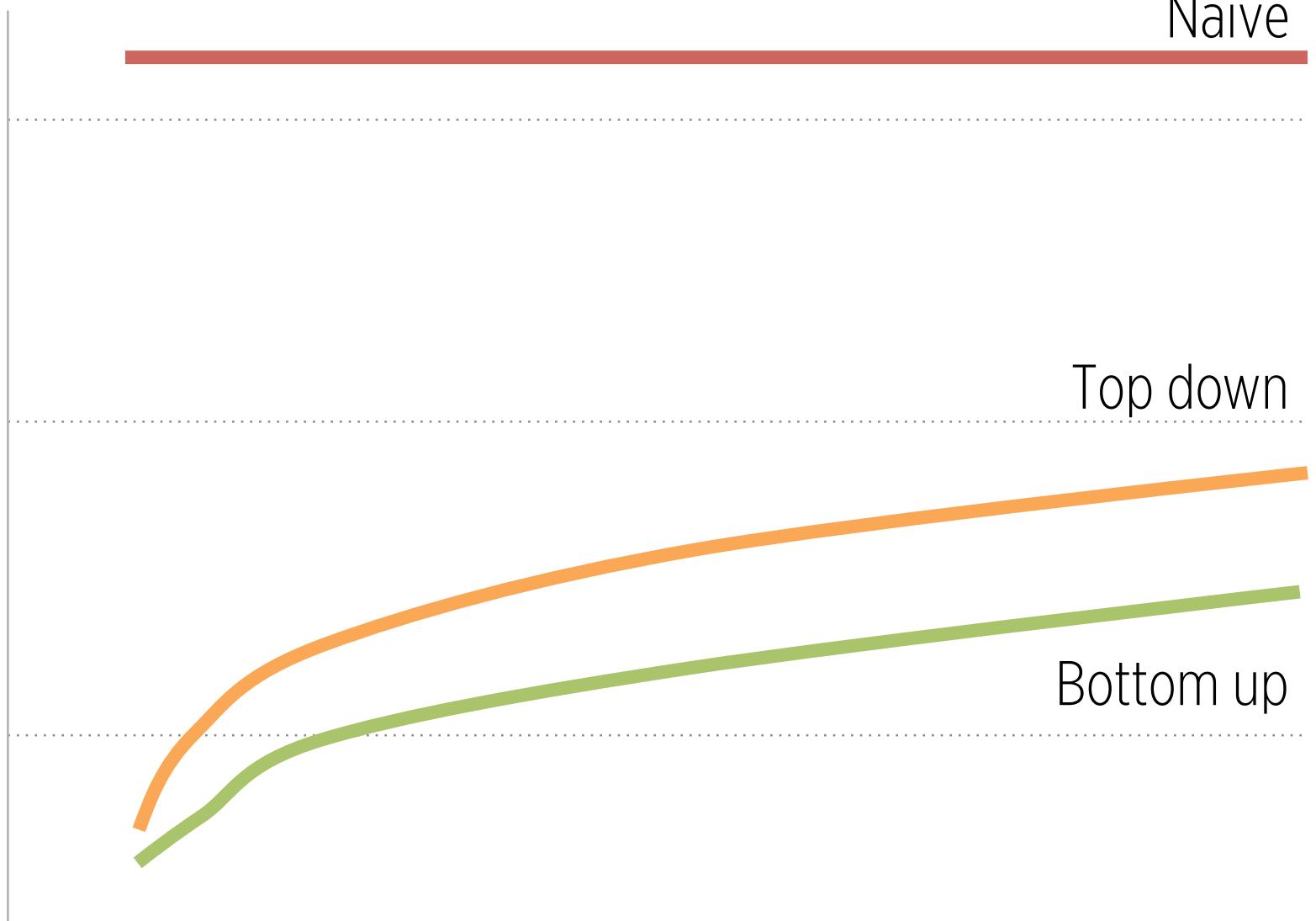
Bottom up

1K

5K

10K

thousand tuples / group



influence metric

that is

accessible to end-users

for

Data cleaning

Data exploration

Provenance reduction

scorpion

eugenewu@mit.edu



scorpion



eugenewu@mit.edu

scorpion

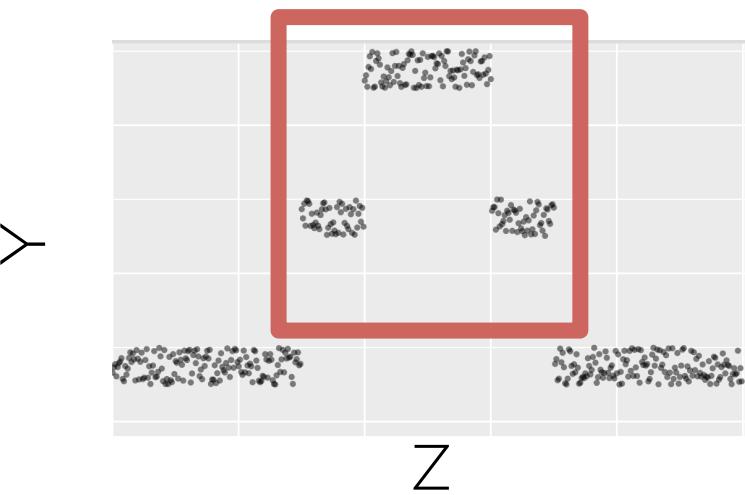
eugenewu@mit.edu



C-parameter

$$\frac{\Delta \text{output} \cdot V}{|p(T)|^c}$$

Low C



High C

